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# Dynamical description of partonic phase at finite chemical potential

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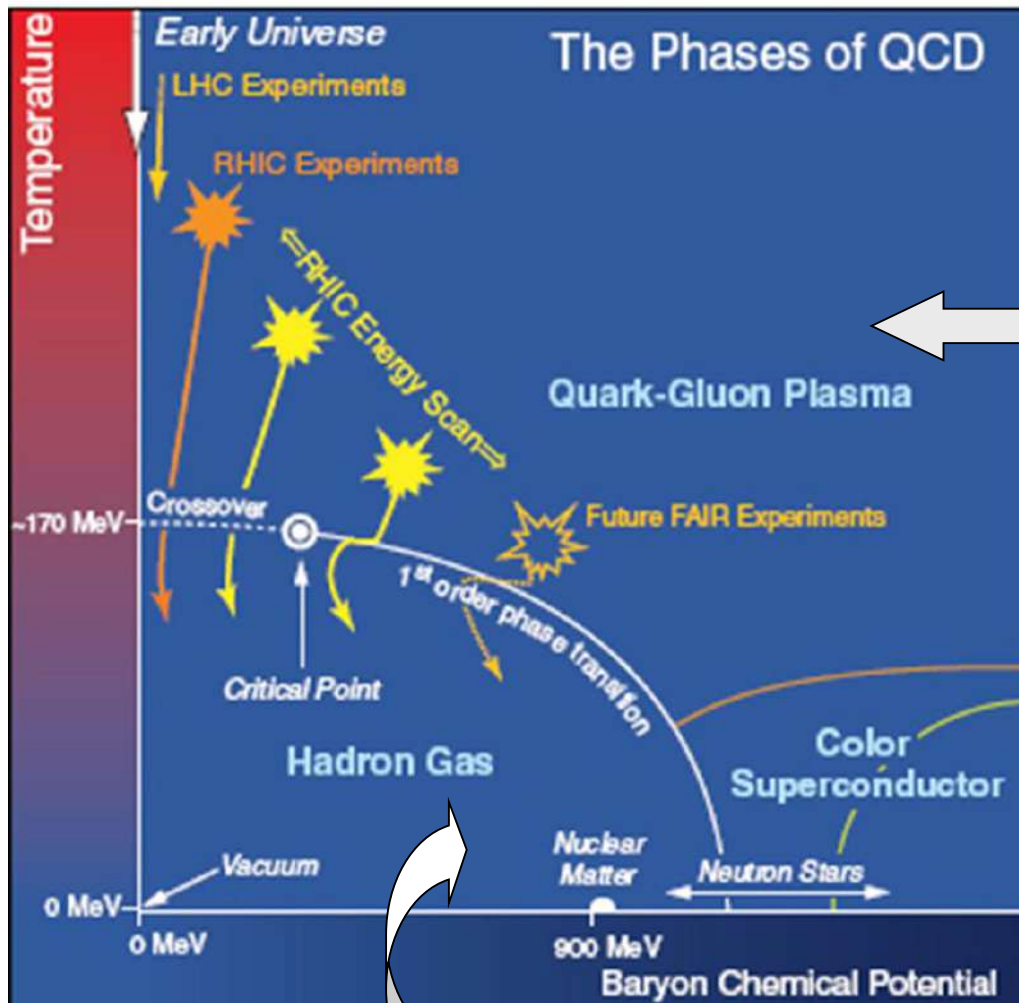


**Pierre Moreau, Olga Soloveva, Lucia Oliva, Taesoo Song, Wolfgang Cassing**

**7th International Symposium on  
Non-equilibrium Dynamics**  
16 - 22 June, 2019, Castiglione della Pescaia, Italy

The banner features a scenic view of a coastline with a castle on a cliff. On the left, there is a map of Italy with a red circle highlighting the location of Castiglione della Pescaia. The 'nED' logo is in the top left corner.

# The ,holy grail' of heavy-ion physics:



## The phase diagram of QCD

- Study of the **phase transition** from hadronic to partonic matter – **Quark-Gluon-Plasma**



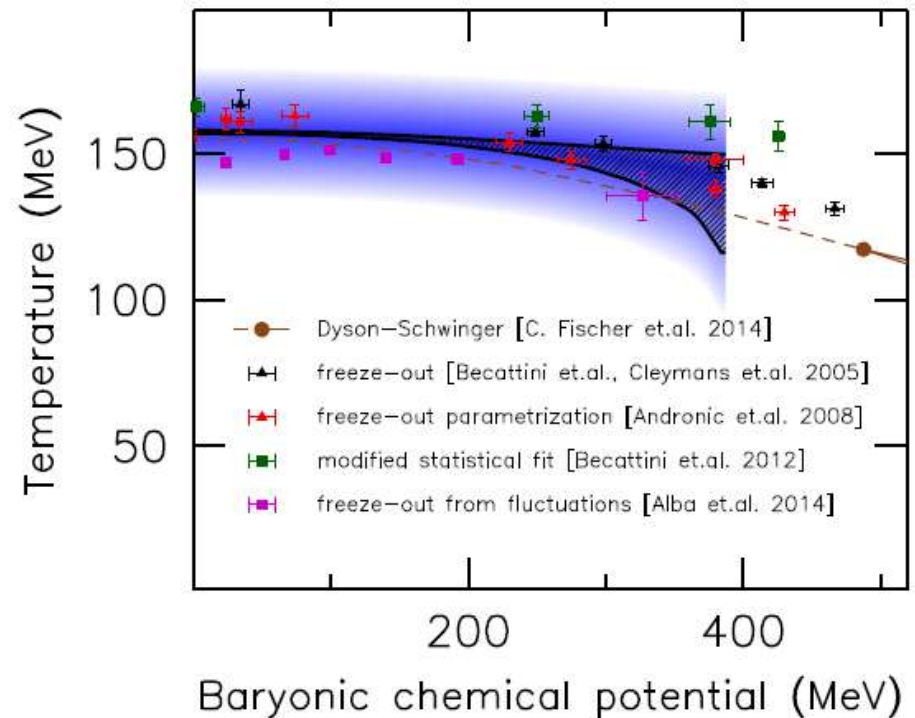
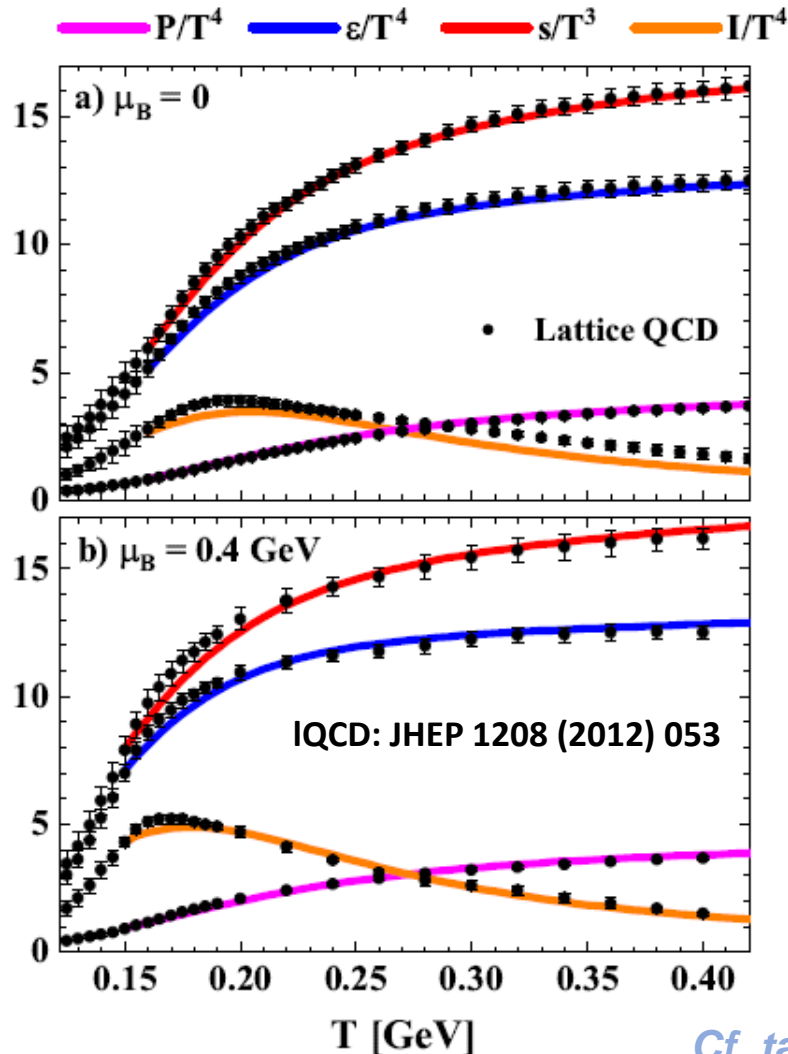
- Search for the **critical point**
- Search for signatures of **chiral symmetry restoration**

- Study of the **in-medium** properties of hadrons at high baryon density and temperature

# Theory: lattice QCD data for $\mu_B = 0$ and finite $\mu_B > 0$

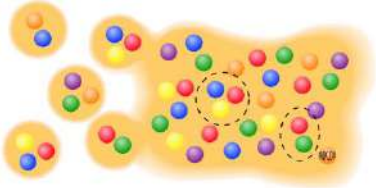
□ Deconfinement phase transition from hadron gas to QGP with increasing T and  $\mu_B$

IQCD: J. Guenther et al., Nucl. Phys. A 967 (2017) 720



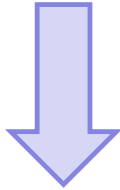
→ Lattice QCD results: up to  $\mu_B < 400 \text{ MeV}$ :  
Crossover: hadron gas → QGP

Cf. talk by Claudia Ratti



# Degrees-of-freedom of QGP

❖ IQCD gives QGP EoS at finite  $\mu_B$

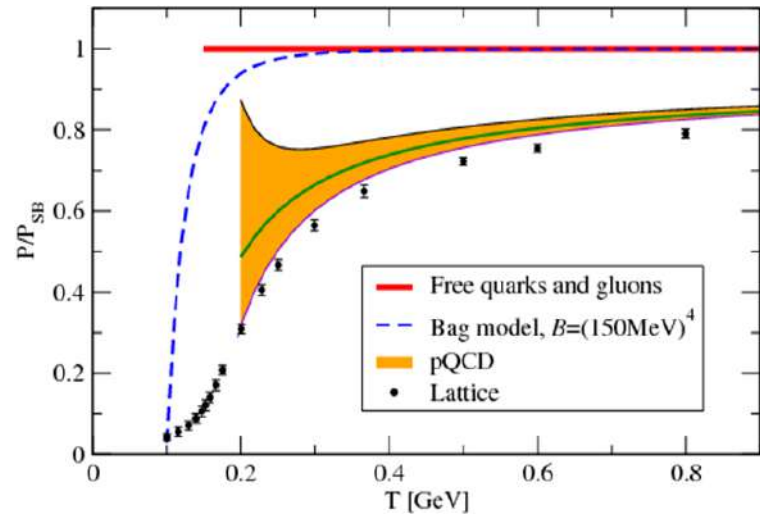


! need to be interpreted in terms of degrees-of-freedom

**pQCD:**

- weakly interacting system
- massless quarks and gluons

❖ How to learn about degrees-of-freedom of QGP ? → HIC experiments



Non-perturbative QCD ← pQCD

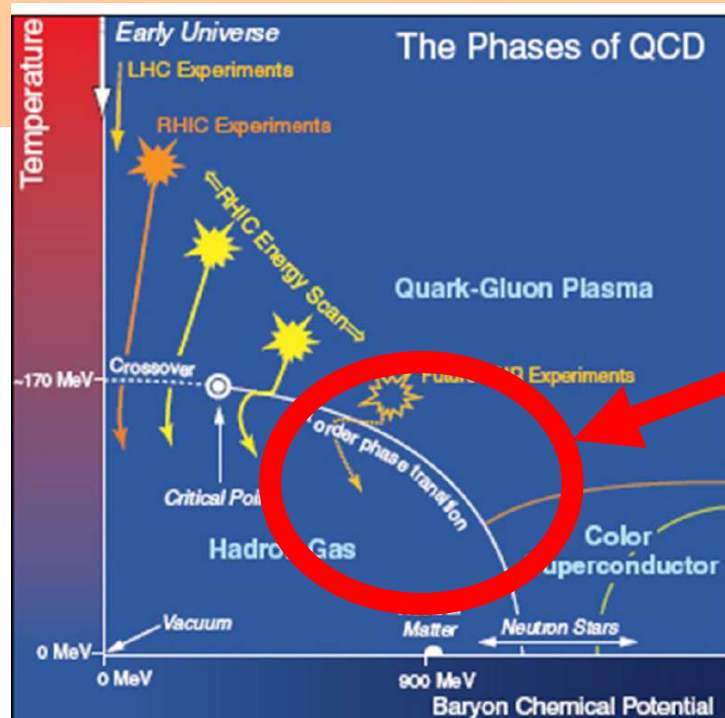


**Thermal QCD**

= QCD at high parton densities:

- strongly interacting system
- massive quarks and gluons
- quasiparticles
- = effective degrees-of-freedom

# DQPM ( $T, \mu_q$ )



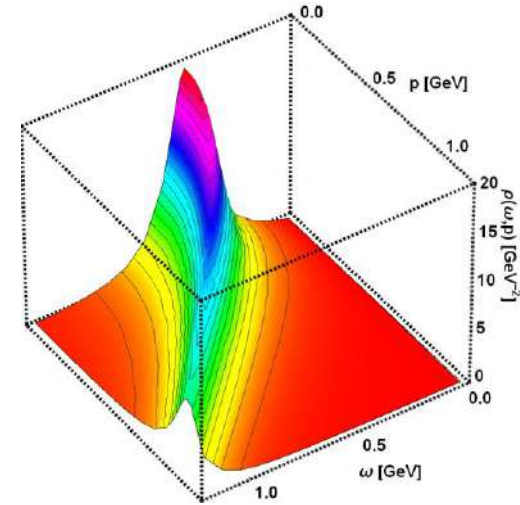
**finite  $\mu_q$**

# Dynamical QuasiParticle Model (DQPM)

- The QGP phase is described in terms of **interacting quasiparticles: quarks and gluons** with Lorentzian spectral functions:

$$\rho_j(\omega, \mathbf{p}) = \frac{\gamma_j}{\tilde{E}_j} \left( \frac{1}{(\omega - \tilde{E}_j)^2 + \gamma_j^2} - \frac{1}{(\omega + \tilde{E}_j)^2 + \gamma_j^2} \right)$$

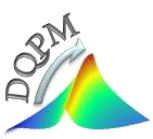
$$\equiv \frac{4\omega\gamma_j}{(\omega^2 - \mathbf{p}^2 - M_j^2)^2 + 4\gamma_j^2\omega^2}$$



- Resummed properties of the quasiparticles are specified by scalar **complex self-energies**:

|   |
|---|
| <p>gluon propagator: <math>\Delta^{-1} = P^2 - \Pi</math>    &amp;    quark propagator <math>S_q^{-1} = P^2 - \Sigma_q</math></p> <p>gluon self-energy: <math>\Pi = M_g^2 - i2g_g\omega</math>    &amp;    quark self-energy: <math>\Sigma_q = M_q^2 - i2g_q\omega</math></p> |
|---|

- Real part of the self-energy: **thermal mass** ( $M_g, M_q$ )
- Imaginary part of the self-energy: **interaction width** of partons ( $\gamma_g, \gamma_q$ )



# Parton properties

- Modeling of the quark/gluon **masses** and **widths** (inspired by HTL calculations)

## Masses:

$$M_{q(\bar{q})}^2(T, \mu_B) = \frac{N_c^2 - 1}{8N_c} g^2(T, \mu_B) \left( T^2 + \frac{\mu_q^2}{\pi^2} \right)$$

$$M_g^2(T, \mu_B) = \frac{g^2(T, \mu_B)}{6} \left( \left( N_c + \frac{1}{2} N_f \right) T^2 + \frac{N_c}{2} \sum_q \frac{\mu_q^2}{\pi^2} \right)$$

## Widths:

$$\gamma_{q(\bar{q})}(T, \mu_B) = \frac{1}{3} \frac{N_c^2 - 1}{2N_c} \frac{g^2(T, \mu_B) T}{8\pi} \ln \left( \frac{2c}{g^2(T, \mu_B)} + 1 \right)$$

$$\gamma_g(T, \mu_B) = \frac{1}{3} N_c \frac{g^2(T, \mu_B) T}{8\pi} \ln \left( \frac{2c}{g^2(T, \mu_B)} + 1 \right)$$

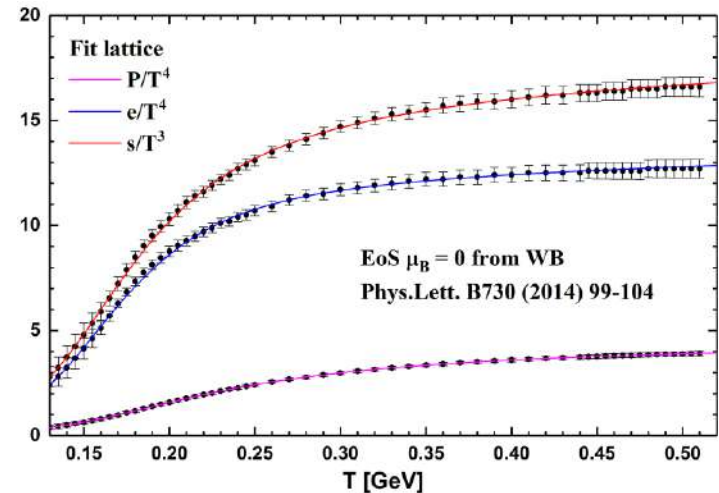
- **Coupling constant:** input: IQCD **entropy density** as a function of temperature for  $\mu_B$   
 → Fit to lattice data at  $\mu_B=0$  with

$$g^2(s/s_{SB}) = d \left( (s/s_{SB})^e - 1 \right)^f$$

$$s_{SB}^{QCD} = 19/9 \pi^2 T^3$$

→ **DQPM :**

only **one parameter** ( $c = 14.4$ )  
 +  $(T, \mu_B)$ - dependent **coupling constant** have to be determined from lattice results



# DQPM at finite $(T, \mu_q)$ : scaling hypothesis

- Scaling hypothesis for the effective temperature  $T^*$  for  $N_f = N_c = 3$

$$\mu_u = \mu_d = \mu_s = \mu_q$$

$$T^{*2} = T^2 + \frac{\mu_q^2}{\pi^2}$$

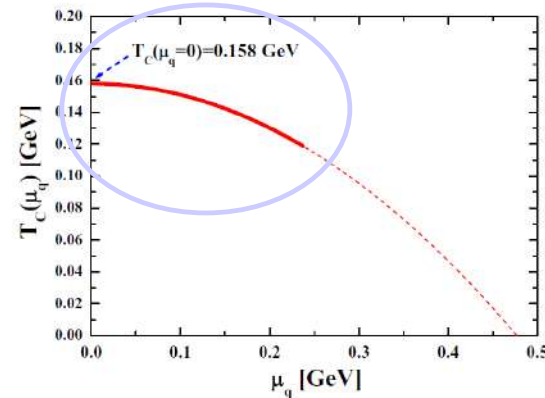
- Coupling constant:

$$g(T/T_c(\mu=0)) \longrightarrow g(T^*/T_c(\mu))$$

- Critical temperature  $T_c(\mu_q)$  : obtained by requiring a constant energy density  $\varepsilon$  for the system at  $T=T_c(\mu_q)$  where  $\varepsilon$  at  $T_c(\mu_q=0)=156$  GeV is fixed by IQCD at  $\mu_q=0$



$$\frac{T_c(\mu_q)}{T_c(\mu_q=0)} = \sqrt{1 - \alpha \mu_q^2} \approx 1 - \alpha/2 \mu_q^2 + \dots$$



$$\alpha \approx 8.79 \text{ GeV}^{-2}$$

**! Consistent with lattice QCD:**

IQCD: C. Bonati et al., PRC90 (2014) 114025

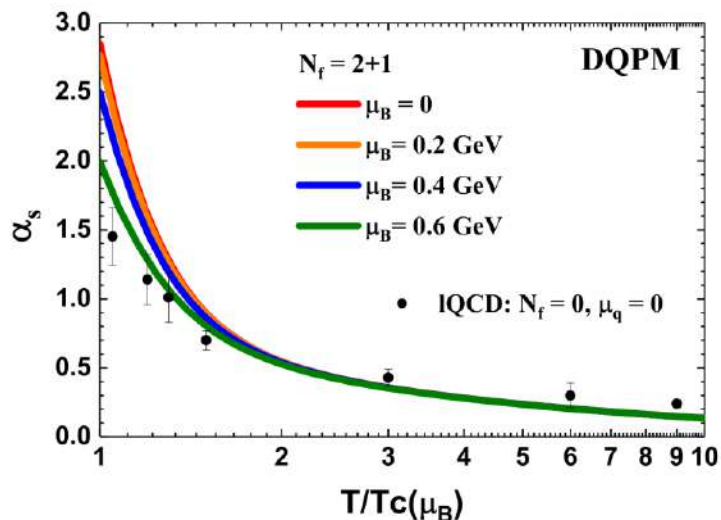
$$\frac{T_c(\mu_B)}{T_c} = 1 - \kappa \left( \frac{\mu_B}{T_c} \right)^2 + \dots$$

$$\text{IQCD } \kappa = 0.013(2) \longleftrightarrow \kappa_{DQPM} \approx 0.0122$$

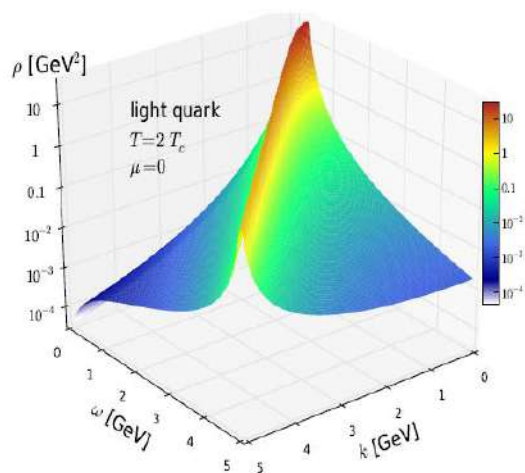
H. Berrehrah et al, PRC 93 (2016) 044914, Int.J.Mod.Phys. E25 (2016) 1642003,

# DQPM: parton properties

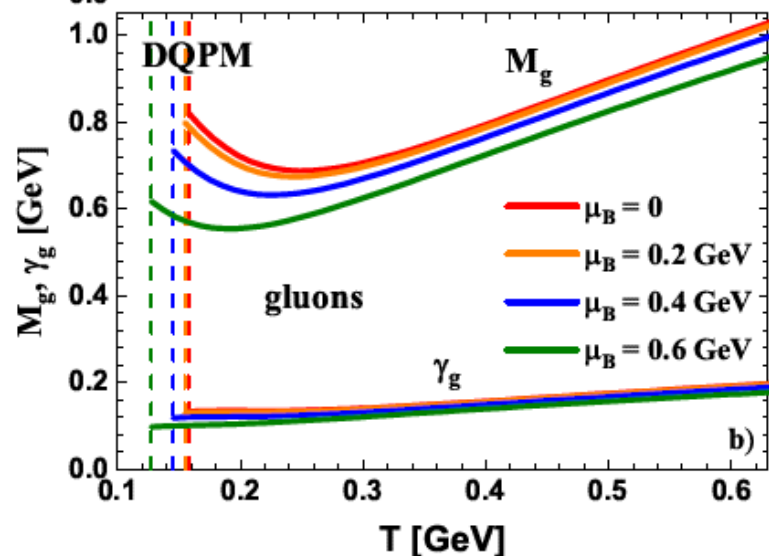
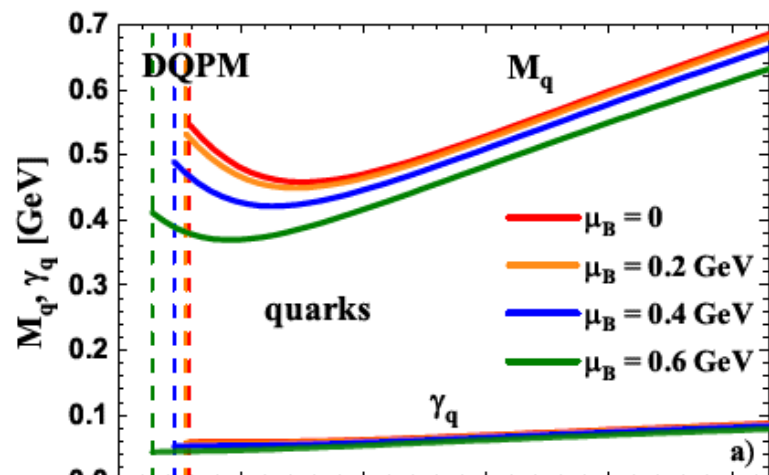
□ Coupling constant as a function of  $(T, \mu_B)$

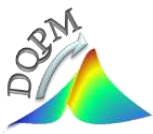


→ Lorentzian spectral function:



□ Masses and widths as a function of  $(T, \mu_B)$





# DQPM Thermodynamics

- Entropy and baryon density in the quasiparticle limit (G. Baym 1998):

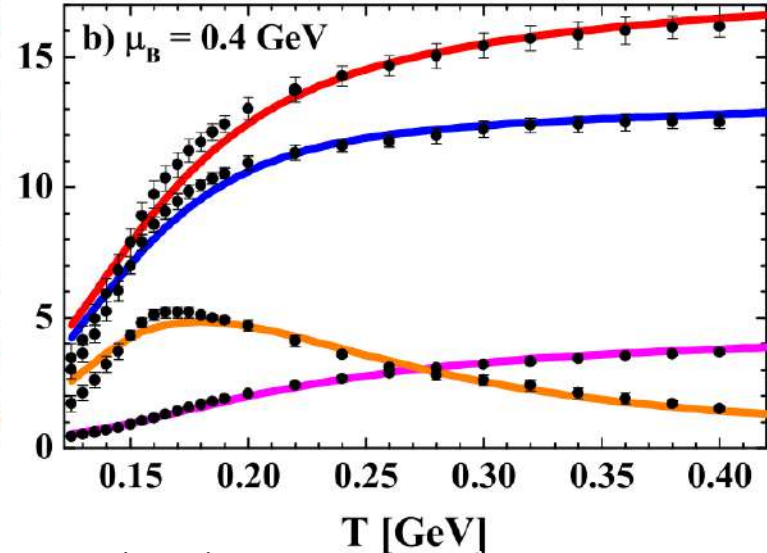
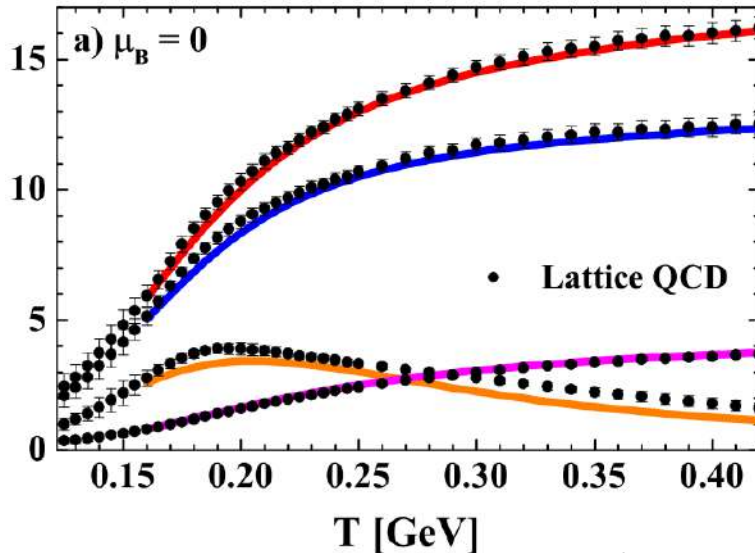
$$s^{dqpm} = - \int \frac{d\omega}{2\pi} \frac{d^3p}{(2\pi)^3} \left[ d_g \frac{\partial n_B}{\partial T} (\text{Im}(\ln -\Delta^{-1}) + \text{Im} \Pi \text{Re} \Delta) \right. \\ \left. + \sum_{q=u,d,s} d_q \frac{\partial n_F(\omega - \mu_q)}{\partial T} (\text{Im}(\ln -S_q^{-1}) + \text{Im} \Sigma_q \text{Re} S_q) \right. \\ \left. + \sum_{\bar{q}=\bar{u},\bar{d},\bar{s}} d_{\bar{q}} \frac{\partial n_F(\omega + \mu_q)}{\partial T} (\text{Im}(\ln -S_{\bar{q}}^{-1}) + \text{Im} \Sigma_{\bar{q}} \text{Re} S_{\bar{q}}) \right]$$

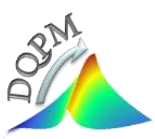
$$n^{dqpm} = - \int \frac{d\omega}{2\pi} \frac{d^3p}{(2\pi)^3} \left[ \sum_{q=u,d,s} d_q \frac{\partial n_F(\omega - \mu_q)}{\partial \mu_q} (\text{Im}(\ln -S_q^{-1}) + \text{Im} \Sigma_q \text{Re} S_q) \right. \\ \left. + \sum_{\bar{q}=\bar{u},\bar{d},\bar{s}} d_{\bar{q}} \frac{\partial n_F(\omega + \mu_q)}{\partial \mu_q} (\text{Im}(\ln -S_{\bar{q}}^{-1}) + \text{Im} \Sigma_{\bar{q}} \text{Re} S_{\bar{q}}) \right]$$

Blairot, Iancu, Rebhan, Phys. Rev. D 63 (2001) 065003



**DQPM:** — P/T<sup>4</sup> — ε/T<sup>4</sup> — s/T<sup>3</sup> — I/T<sup>4</sup>





# DQPM EoS at finite $(T, \mu_B)$

Taylor series of thermodynamic quantities in terms of  $(\mu_B/T)$

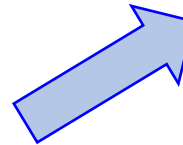
For the pressure:

$$\frac{P(T, \mu_B)}{T^4} = \sum_{n=0} \frac{1}{n!} \chi_B^n \left(\frac{\mu_B}{T}\right)^n$$

with the **baryon number susceptibilities** defined as:

$$\chi_B^n = \left. \frac{\partial^n P}{\partial \mu_B^n} \right|_{\mu_B=0}$$

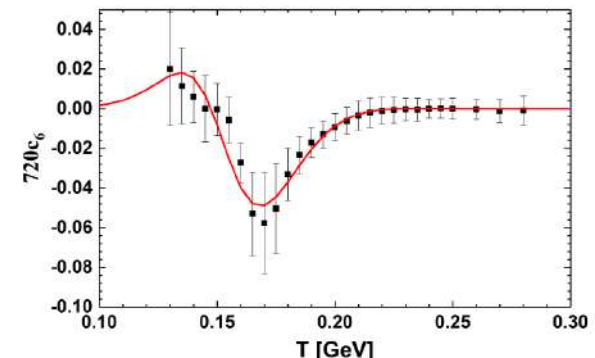
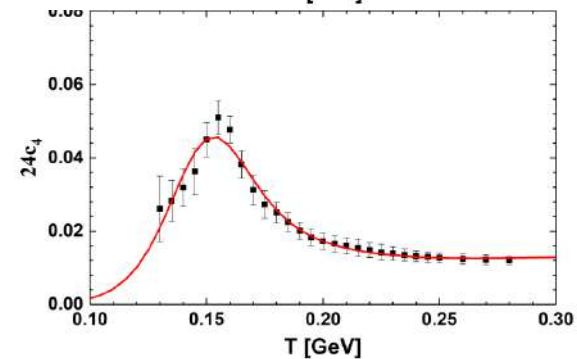
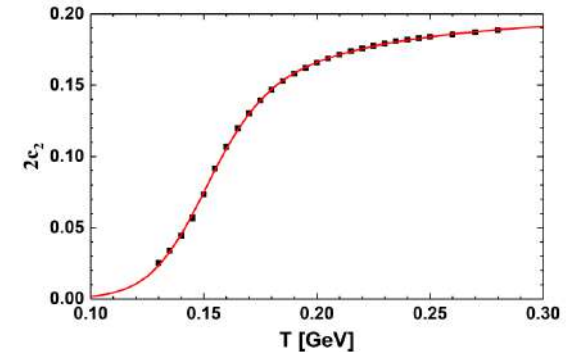
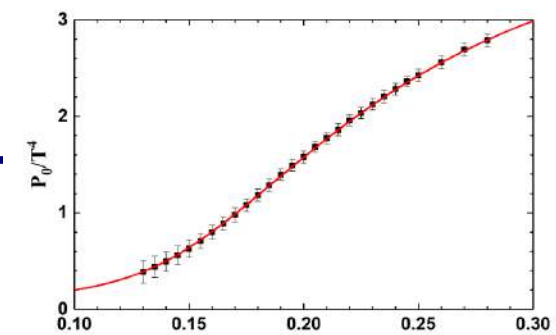
Cf. talk by Claudia Ratti

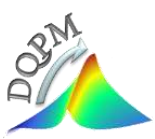


Recent IQCD results - with the 6<sup>th</sup> order susceptibility

$$\frac{P}{T^4} = c_0(T) + c_2(T) \left(\frac{\mu_B}{T}\right)^2 + c_4(T) \left(\frac{\mu_B}{T}\right)^4 + c_6(T) \left(\frac{\mu_B}{T}\right)^6 + \mathcal{O}(\mu_B^8)$$

WB IQCD: J. Günther, R. Bellwied, S. Borsanyi, Z. Fodor, S. D. Katz, A. Pasztor, C. Ratti, EPJ Web Conf. 137, 07008 (2017) 158





# DQPM: Isentropic trajectories for $(T, \mu_B)$

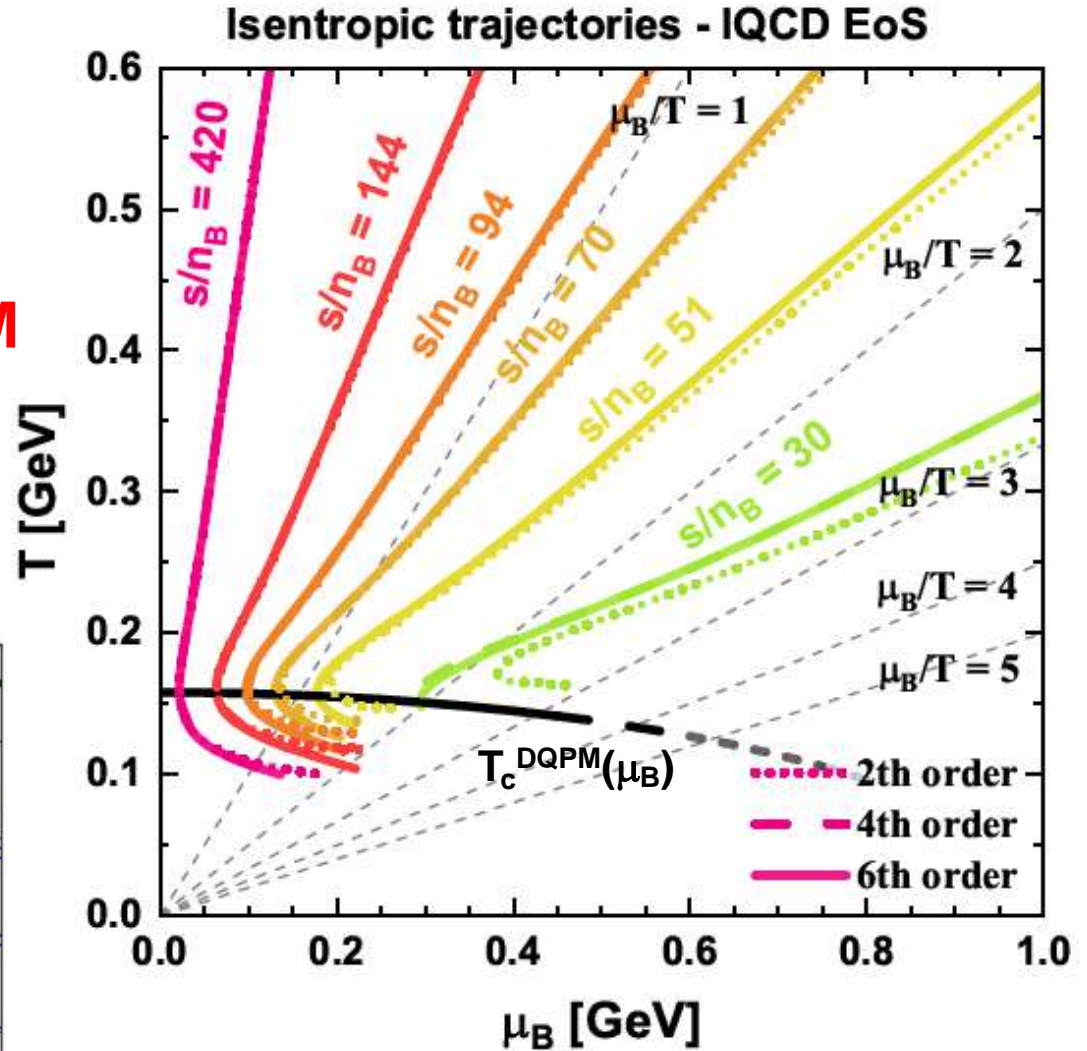
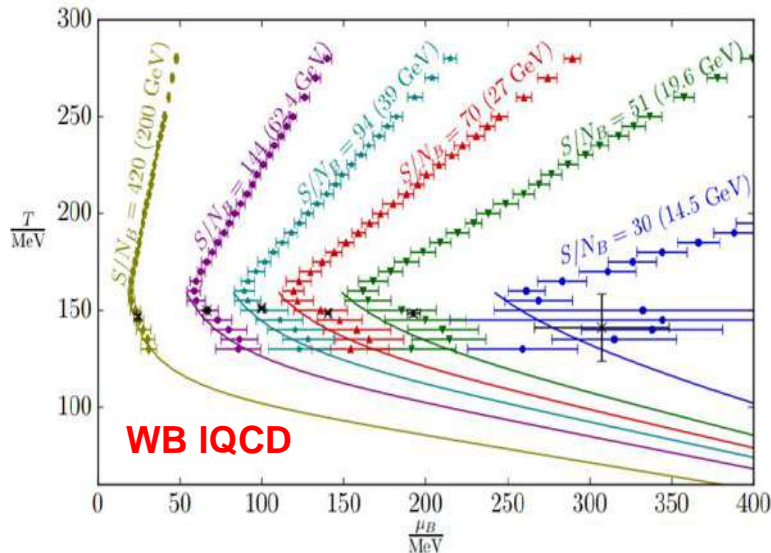
- Correspondance  $s/n_B \leftrightarrow$  collisional energy

$s/n_B = 420 \leftrightarrow 200 \text{ GeV}$   
 $= 144 \leftrightarrow 62.4 \text{ GeV}$   
 $= 94 \leftrightarrow 39 \text{ GeV}$   
 $= 70 \leftrightarrow 27 \text{ GeV}$   
 $= 51 \leftrightarrow 19.6 \text{ GeV}$   
 $= 30 \leftrightarrow 14.5 \text{ GeV}$

**DQPM**

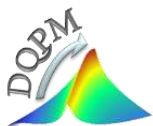


- Safe for  $(\mu_B/T) < 2$



P. Moreau et al., arXiv:1903.10257, PRC (2019)

# **QGP in DQPM: partonic interactions**



# Partonic interactions

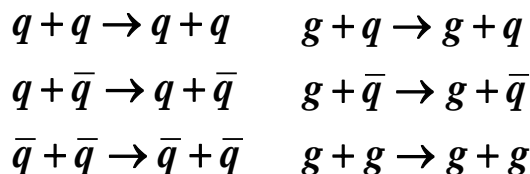
## Reminder (2013): DQPM(T) in PHSD 4.0

DQPM provides the **total width**  $\Gamma$  of the dynamical quasiparticles

$$\Gamma_{total} = \Gamma_{elastic} + \Gamma_{inelastic}$$

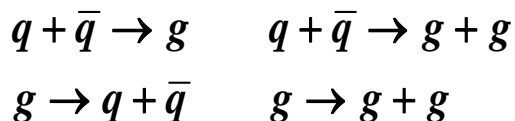
- obtain the **partial widths** (i.e. cross sections) for different channels from the PHSD simulations in the box: transition rates  $\leftrightarrow$  DQPM width

- **(quasi-) elastic collisions:**

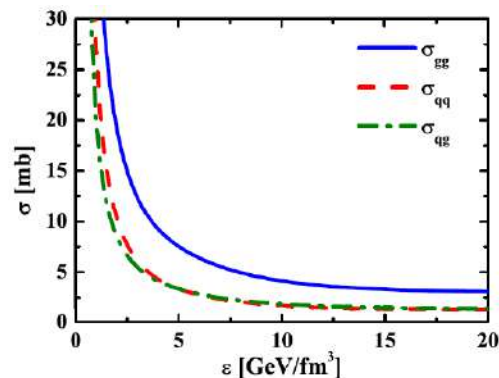


$$\rightarrow \sigma_i(\varepsilon)$$

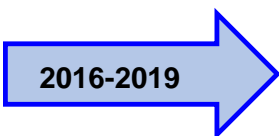
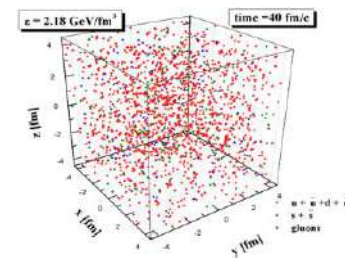
- **inelastic collisions:**



$$\sigma_{q\bar{q} \rightarrow g}(s, \varepsilon, M_q, M_{\bar{q}}) = \frac{2}{4} \frac{4\pi s \Gamma_g^2(\varepsilon)}{[s - M_g^2(\varepsilon)]^2 + s \Gamma_g^2(\varepsilon)} \frac{1}{P_{rel}^2}$$



V. Ozvenchuk et al.,  
PRC 87 (2013) 024901,  
PRC 87 (2013) 064903



To improve the description of QGP dynamics in PHSD we need:  
**off-shell differential and total cross sections**  $\sigma_i(s, m_1, m_2, T, \mu_q)$   
for all combinations  $i = (\text{flavor, spin, color})$

H. Berrehrah et al, PRC 93 (2016) 044914,  
Int.J.Mod.Phys. E25 (2016) 1642003,



P. Moreau et al., arXiv:1903.10257, PRC (2019)

PHSD 5.0

# Partonic interactions: matrix elements

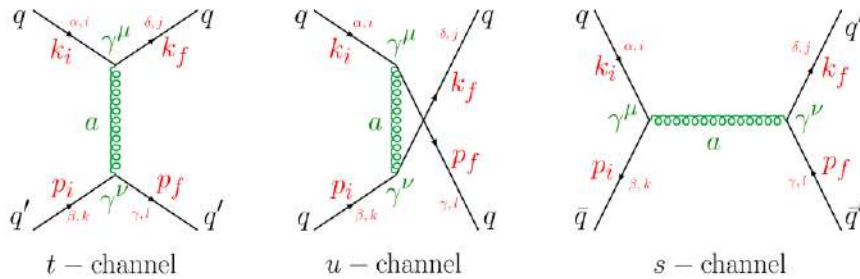
DQPM partonic cross sections  $\rightarrow$  **leading order diagrams**

**Propagators** for massive bosons and fermions:

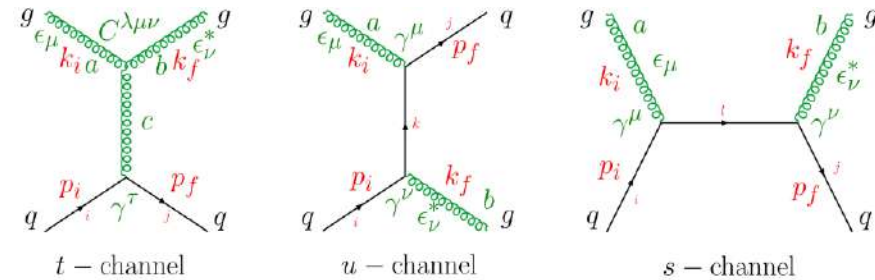
$$\frac{\mu, a}{\text{boson}} \frac{\nu, b}{q} = -i\delta_{ab} \frac{g^{\mu\nu} - q^\mu q^\nu / M_g^2}{q^2 - M_g^2 + 2i\gamma_g q_0}$$

$$\frac{i}{\text{fermion}} \frac{j}{q} = i\delta_{ij} \frac{\not{q} + M_q}{q^2 - M_q^2 + 2i\gamma_q q_0}$$

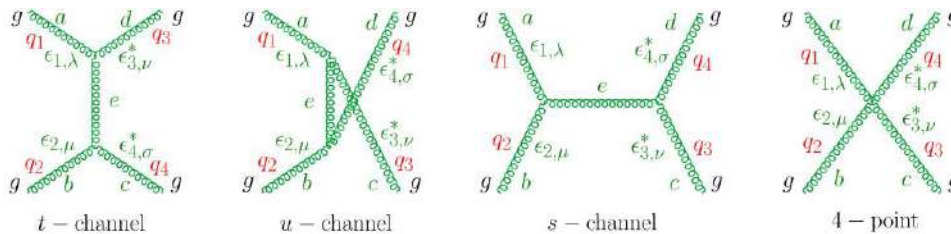
**qq'  $\rightarrow$  qq' scattering**



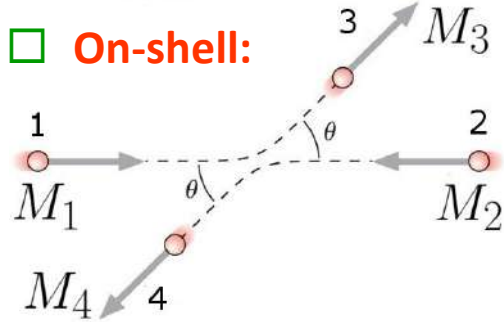
**gq  $\rightarrow$  gq scattering**



**gg  $\rightarrow$  gg scattering**

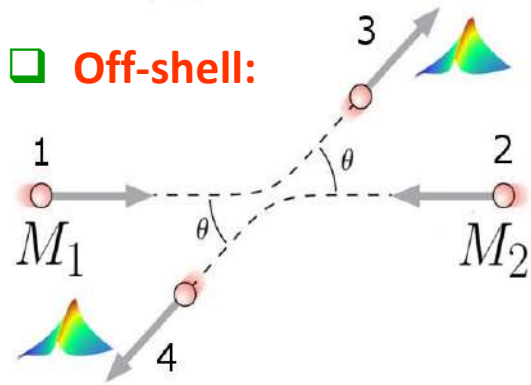


# Differential cross section



**Initial masses: pole masses**

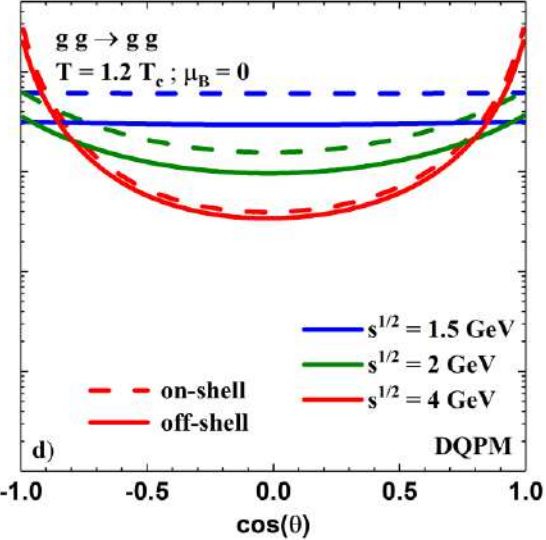
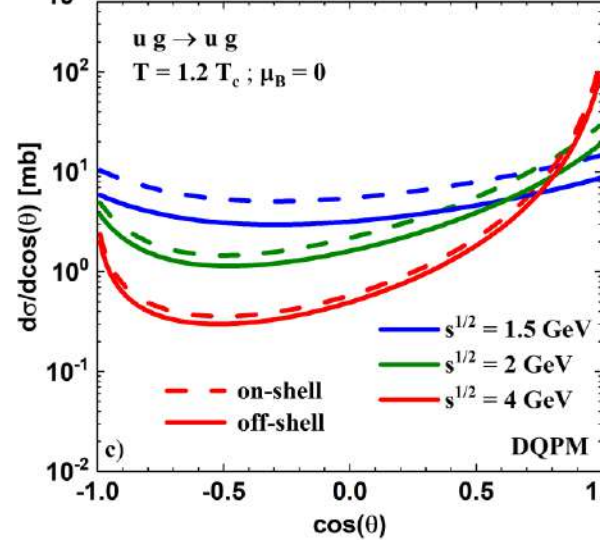
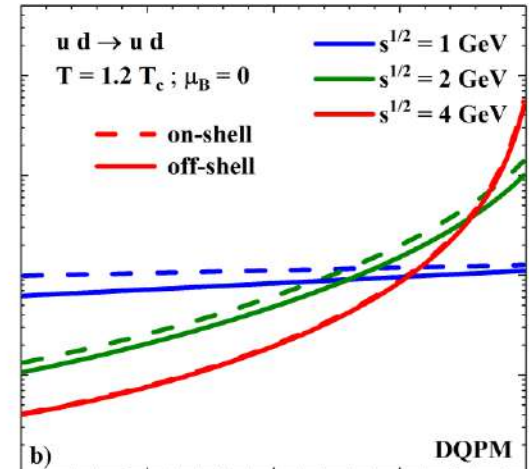
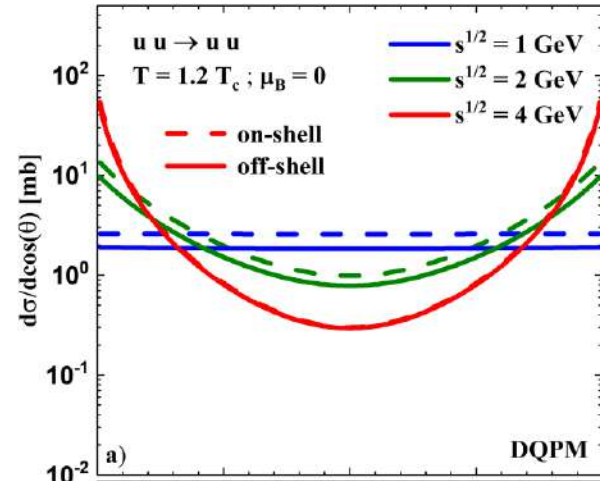
**Final masses: pole masses**



**Initial masses: pole masses**

**Final masses: integrated over spectral functions**

- At lower  $s$ : off-shell  $\sigma <$  on-shell  $\sigma$  since  $\omega_3 + \omega_4 < \sqrt{s}$



**DQPM ( $T, \mu_q$ ):**  
**transport properties at finite ( $T, \mu_q$ )**

# Off-shell collision rate

$$\begin{aligned} \Gamma_i^{\text{off}}(T, \mu_q) &= \frac{d_i}{n_i^{\text{off}}(T, \mu_q)} \int \frac{d^4 p_i}{(2\pi)^4} \theta(\omega_i) \tilde{\rho}_i f_i(\omega_i, T, \mu_q) \\ &\times \sum_{j=q, \bar{q}, g} \int \frac{d^4 p_j}{(2\pi)^4} \theta(\omega_j) d_j \tilde{\rho}_j f_j \\ &\times \int \frac{d^4 p_3}{(2\pi)^4} \theta(\omega_3) \tilde{\rho}_3 \int \frac{d^4 p_4}{(2\pi)^4} \theta(\omega_4) \tilde{\rho}_4 (1 \pm f_3)(1 \pm f_4) \\ &\times \underbrace{|\bar{\mathcal{M}}|^2(p_i, p_j, p_3, p_4)}_{\text{circled}} (2\pi)^4 \delta^{(4)}(p_i + p_j - p_3 - p_4), \end{aligned}$$

➤ **off-shell density**

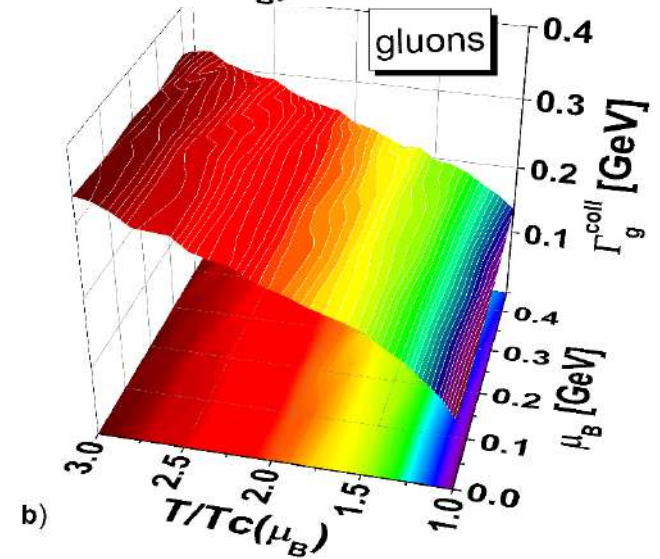
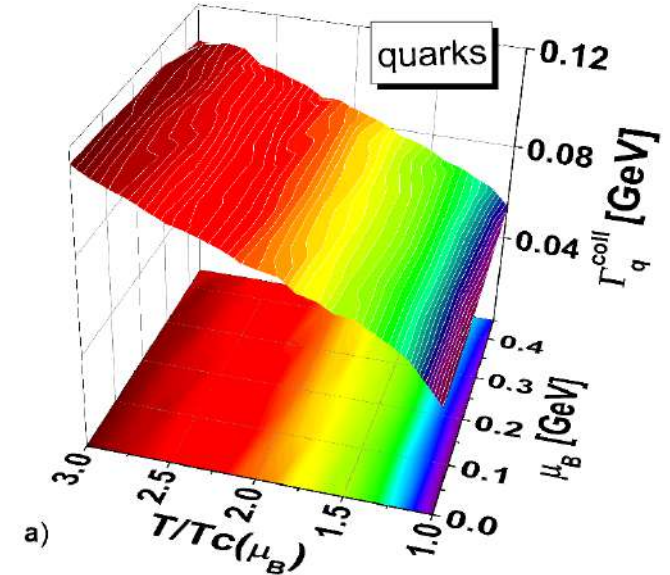
$$n_i^{\text{off}}(T, \mu_q) = d_i \int \frac{d^4 p_i}{(2\pi)^4} \theta(\omega_i) 2\omega_i \tilde{\rho}_i f_i(T, \mu_q)$$

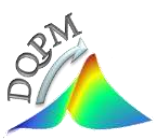
➤ **renormalized spectral-function for the time-like sector**

$$\tilde{\rho}_j(\omega_j, \mathbf{p}_j) = \frac{\rho(\omega_j, \mathbf{p}_j) \theta(p_j^2)}{\int_0^\infty \frac{d\omega_j}{(2\pi)} 2\omega_j \rho(\omega_j, \mathbf{p}_j) \theta(p_j^2)}$$

normalized to 1 and

$$\lim_{\gamma_j \rightarrow 0} \rho_j(\omega, \mathbf{p}) = 2\pi \delta(\omega^2 - \mathbf{p}^2 - M_j^2)$$





# Transport coefficients: shear viscosity

## ➤ Kubo formalism

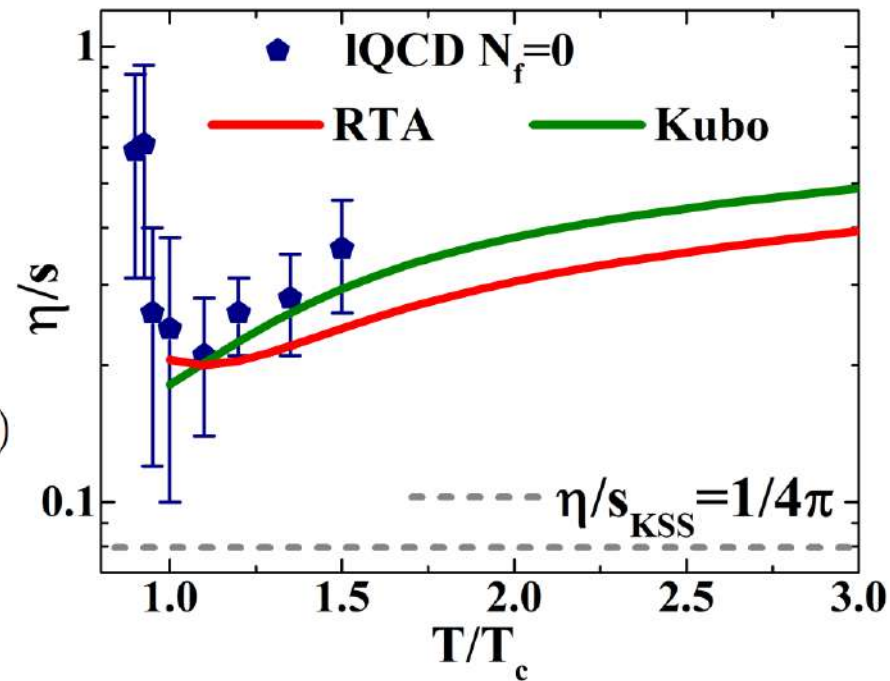
$$\eta^{\text{Kubo}}(T, \mu_q) = - \int \frac{d^4 p}{(2\pi)^4} p_x^2 p_y^2 \sum_{i=q, \bar{q}, g} d_i \frac{\partial f_i(\omega)}{\partial \omega} \rho_i(\omega, \mathbf{p})^2$$

$$= \frac{1}{15T} \int \frac{d^4 p}{(2\pi)^4} \mathbf{p}^4 \sum_{i=q, \bar{q}, g} d_i ((1 \pm f_i(\omega)) f_i(\omega)) \rho_i(\omega, \mathbf{p})^2$$

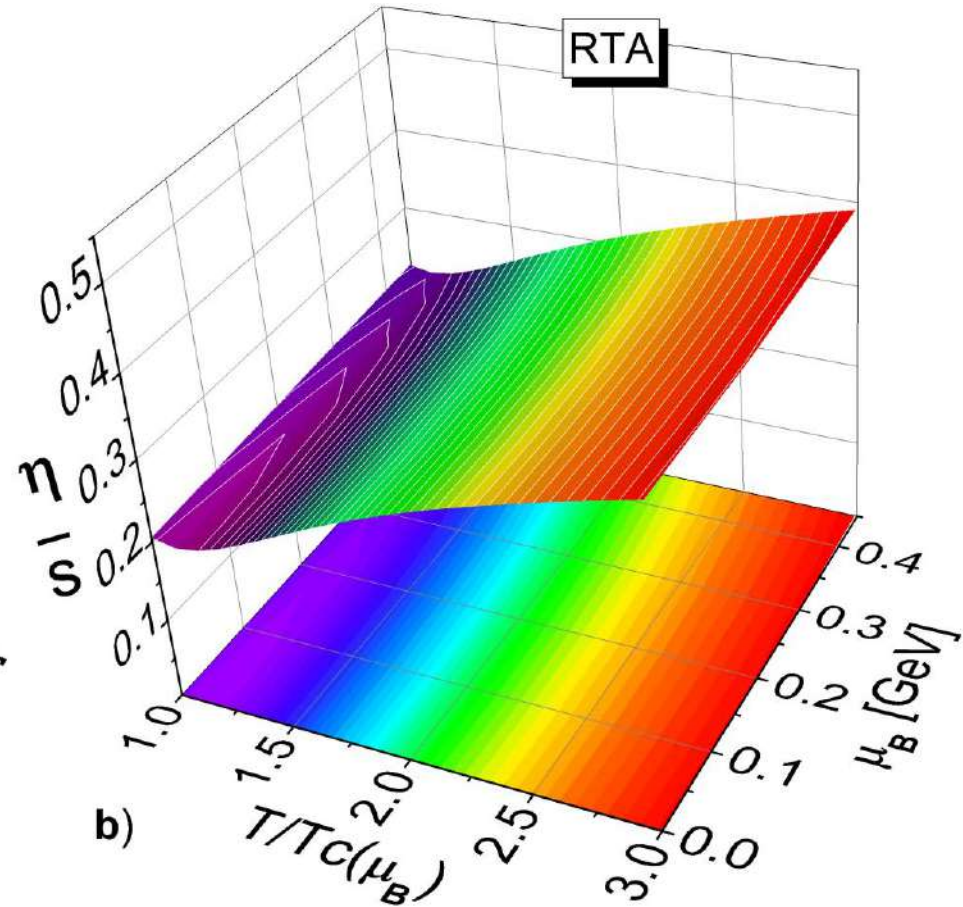
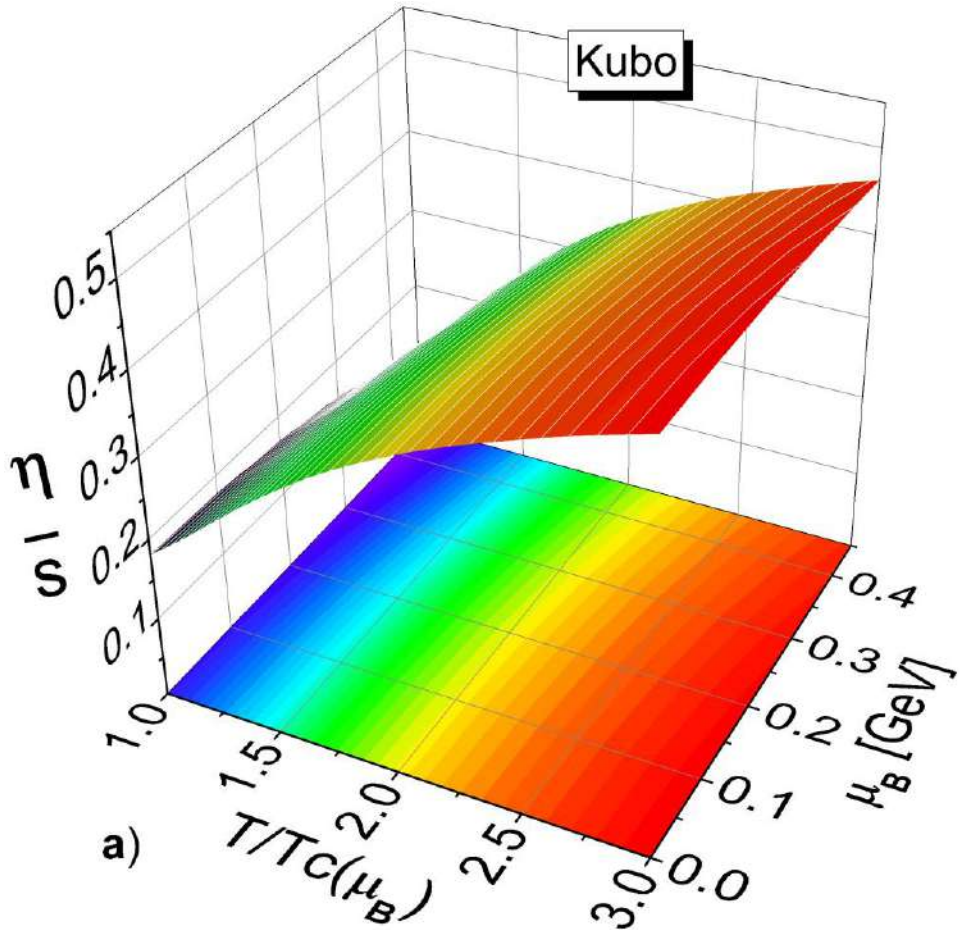
## ➤ Relaxation Time Approximation

$$\eta^{\text{RTA}}(T, \mu_q) = \frac{1}{15T} \int \frac{d^3 p}{(2\pi)^3} \sum_{i=q, \bar{q}, g} \left( \frac{\mathbf{p}^4}{E_i^2 \Gamma_i(\mathbf{p}_i, T, \mu_q)} d_i ((1 \pm f_i(E_i)) f_i(E_i)) \right) + \mathcal{O}(\Gamma_i)$$

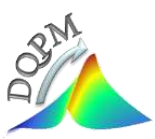
Rate  $\Gamma$  (all diagrams for  $M$  in the pole mass)  
 For on-shell case ( $\rho \rightarrow \delta$ )  $\Gamma = 2\gamma$ ,  $\gamma$  – collisional width



# Transport coefficients: shear viscosity



➤ Very weak  $\mu_B$  dependence



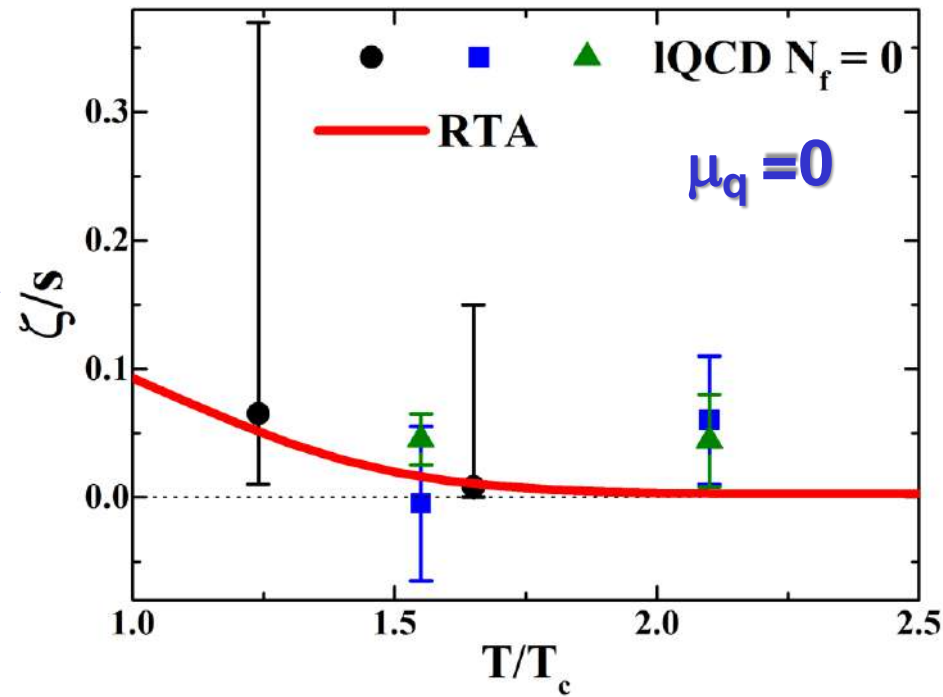
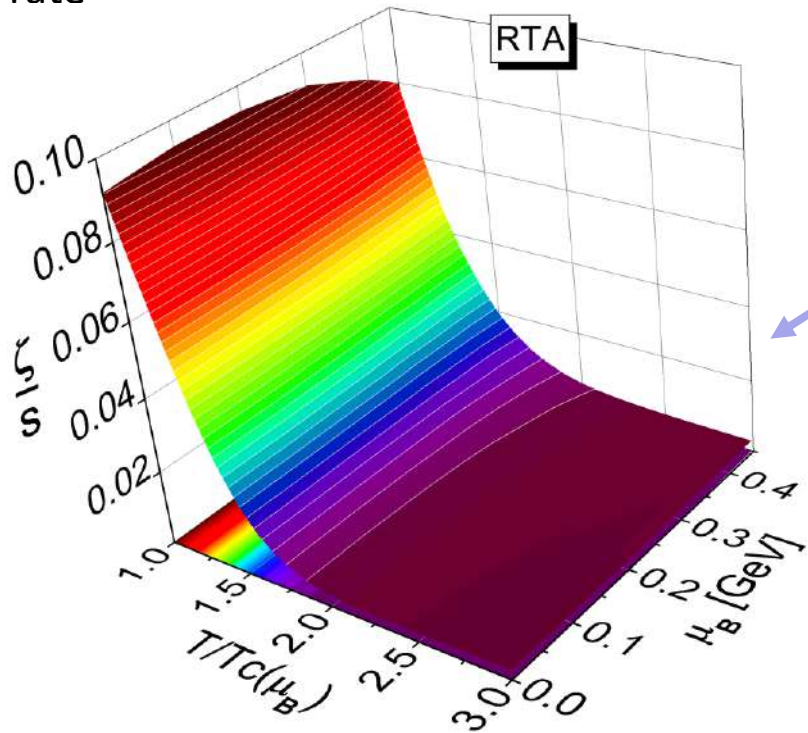
# Transport coefficients: bulk viscosity

## Relaxation Time Approximation

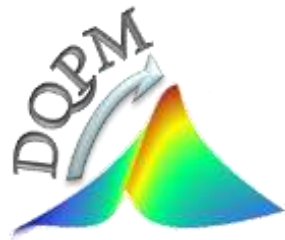
$$\zeta^{\text{RTA}}(T, \mu_q) = \frac{1}{9T} \int \frac{d^3p}{(2\pi)^3} \sum_{i=q, \bar{q}} \left( \frac{\mathbf{p}^4}{E_i^2 \Gamma_i(\mathbf{p}_i, T, \mu_q)} d_i ((1 \pm f_i(E_i)) f_i(E_i)) \right) \left[ \mathbf{p}^2 - 3c_s^2 \left( E_i^2 - T^2 \frac{dm_q^2}{dT^2} \right) \right]^2$$

from DQPM parametrization

rate



**QGP:**  
**in-equilibrium → off-equilibrium**



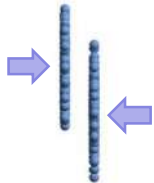


# Parton-Hadron-String-Dynamics (PHSD)

**PHSD** is a **non-equilibrium microscopic transport approach** for the description of **strongly-interacting hadronic and partonic matter** created in heavy-ion collisions

**Dynamics:** based on the solution of **generalized off-shell transport equations** derived from Kadanoff-Baym many-body theory

Initial A+A collision



Initial A+A collisions :

$N+N \rightarrow$  **string formation**  $\rightarrow$  decay to pre-hadrons + leading hadrons

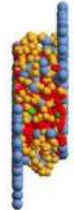
Formation of QGP stage if local  $\varepsilon > \varepsilon_{\text{critical}}$  :

dissolution of **pre-hadrons**  $\rightarrow$  partons

Partonic phase - QGP:

QGP is described by the **Dynamical QuasiParticle Model (DQPM)** matched to reproduce **lattice QCD EoS** for finite  $T$  and  $\mu_B$  (crossover)

Partonic phase



- **Degrees-of-freedom:** strongly interacting quasiparticles:

**massive quarks and gluons ( $g, q, q_{\text{bar}}$ )** with sizeable collisional widths in a self-generated mean-field potential

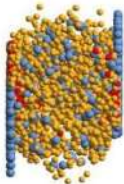
- **Interactions:** (quasi-)elastic and inelastic collisions of partons

**Hadronization** to colorless **off-shell mesons and baryons:**

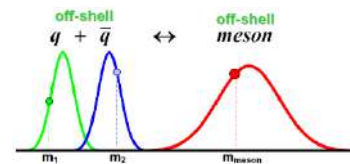
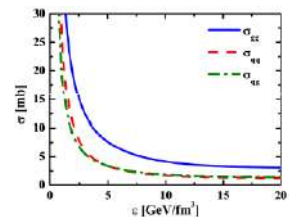
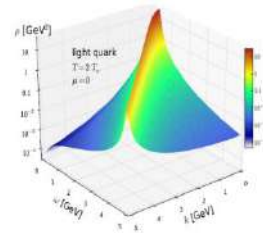
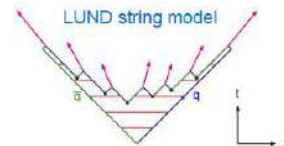
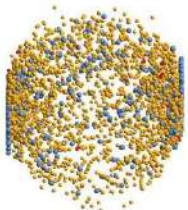
Strict 4-momentum and quantum number conservation

**Hadronic phase:** hadron-hadron interactions – **off-shell HSD**

Hadronization



Hadronic phase





# Extraction of $(T, \mu_B)$ in PHSD

- In each space-time cell of the PHSD, the **energy-momentum tensor** is calculated by the formula:

$$T^{\mu\nu} = \sum_i \frac{p_i^\mu p_i^\nu}{E_i}$$

- Diagonalization of the energy-momentum tensor to get the energy density and pressure components expressed in **the local rest frame (LRF)**

$$T^{\mu\nu} = \begin{pmatrix} T^{00} & T^{01} & T^{02} & T^{03} \\ T^{10} & T^{11} & T^{12} & T^{13} \\ T^{20} & T^{21} & T^{22} & T^{23} \\ T^{30} & T^{31} & T^{32} & T^{33} \end{pmatrix} \rightarrow \begin{pmatrix} \epsilon^{LRF} & 0 & 0 & 0 \\ 0 & P_x^{LRF} & 0 & 0 \\ 0 & 0 & P_y^{LRF} & 0 \\ 0 & 0 & 0 & P_z^{LRF} \end{pmatrix}$$

For **each space-time cell** of the PHSD:

- Calculate the local energy density  $\epsilon^{\text{PHSD}}$  and baryon density  $n_B^{\text{PHSD}}$

- use IQCD relations (up to 4<sup>th</sup> order):
 
$$\left\{ \begin{array}{l} \frac{n_B}{T^3} \approx \chi_2^B(T) \left( \frac{\mu_B}{T} \right) + \dots \\ \Delta\epsilon/T^4 \approx \frac{1}{2} \left( T \frac{\partial \chi_2^B(T)}{\partial T} + 3\chi_2^B(T) \right) \left( \frac{\mu_B}{T} \right)^2 + \dots \end{array} \right.$$

➔ obtain  $(T, \mu_B)$  by solving the system of coupled equations using  $\epsilon^{\text{PHSD}}$  and  $n_B^{\text{PHSD}}$



# Extraction of $(T, \mu_B)$ in PHSD

For each space-time cell of the PHSD:

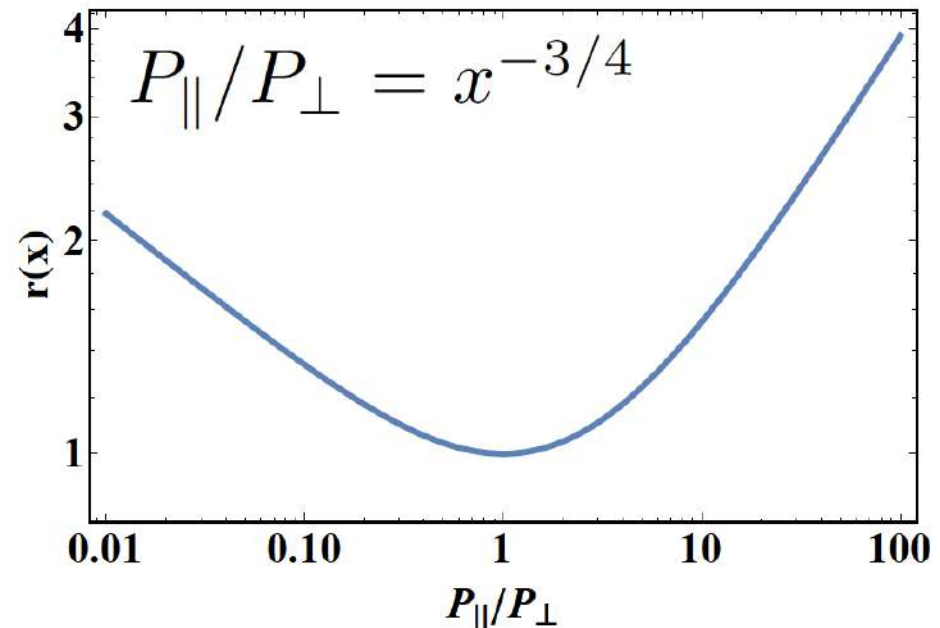
- Correction for the medium anisotropy to extract values for  $(T, \mu_B)$

$$\epsilon^{\text{anis}} = \epsilon^{\text{EoS}} r(x)$$

$$P_{\perp} = P^{\text{EoS}} [r(x) + 3xr'(x)]$$

$$P_{\parallel} = P^{\text{EoS}} [r(x) - 6xr'(x)]$$

$$r(x) = \begin{cases} \frac{x^{-1/3}}{2} \left[ 1 + \frac{x \operatorname{arctanh} \sqrt{1-x}}{\sqrt{1-x}} \right] & \text{for } x \leq 1 \\ \frac{x^{-1/3}}{2} \left[ 1 + \frac{x \operatorname{arctan} \sqrt{x-1}}{\sqrt{x-1}} \right] & \text{for } x \geq 1 \end{cases}$$



Ryblewski, Florkowski, Phys.Rev. C85 (2012) 064901

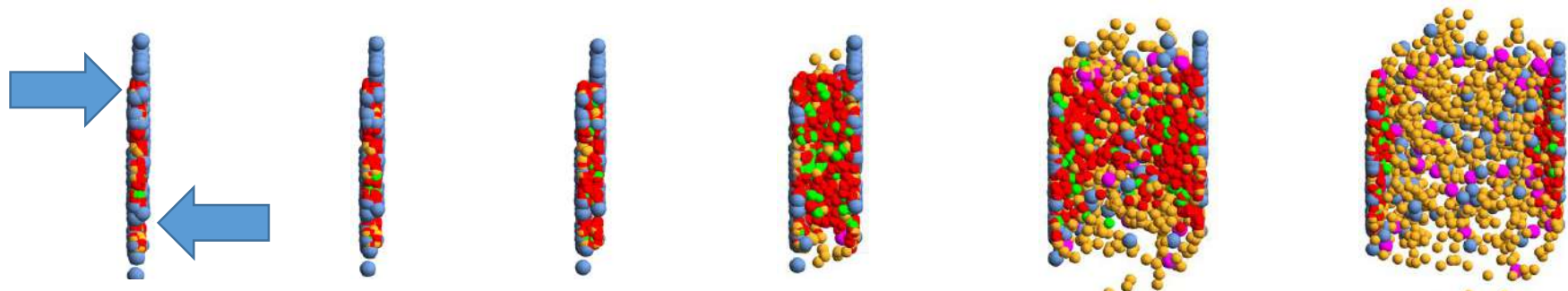
- We have to solve the following system in PHSD:

Done by Newton-Raphson method

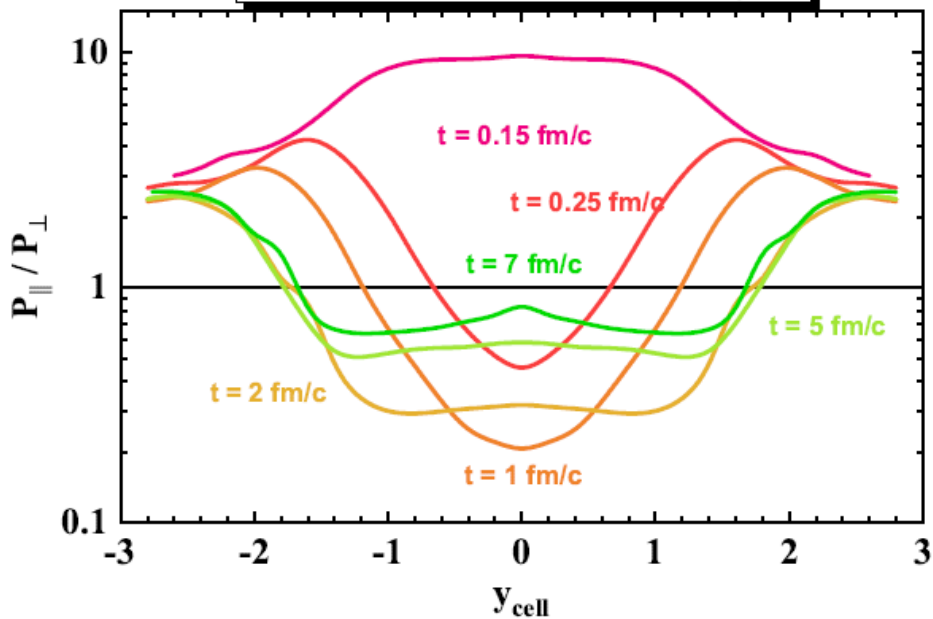
$$\begin{cases} \epsilon^{\text{EoS}}(T, \mu_B) = \epsilon^{\text{PHSD}} / r(x) \\ n_B^{\text{EoS}}(T, \mu_B) = n_B^{\text{PHSD}} \end{cases}$$



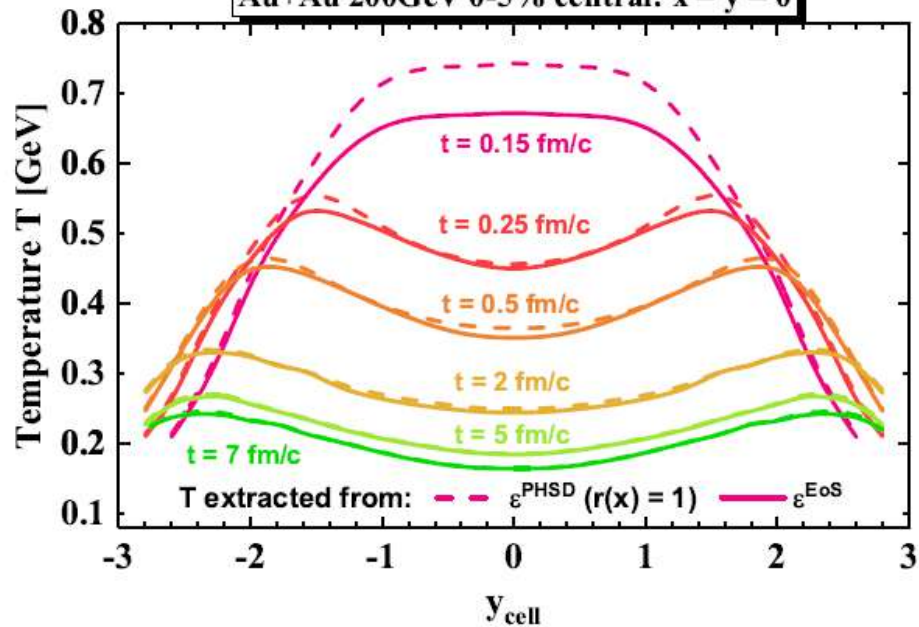
# T, P in HIC ( $\sqrt{s_{NN}} = 200$ GeV)



Au+Au 200GeV 0-5% central:  $x = y = 0$



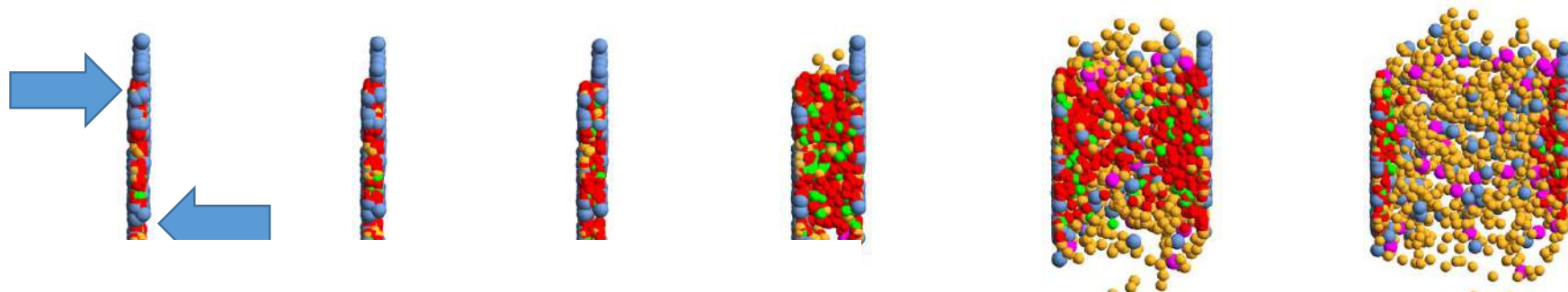
Au+Au 200GeV 0-5% central:  $x = y = 0$



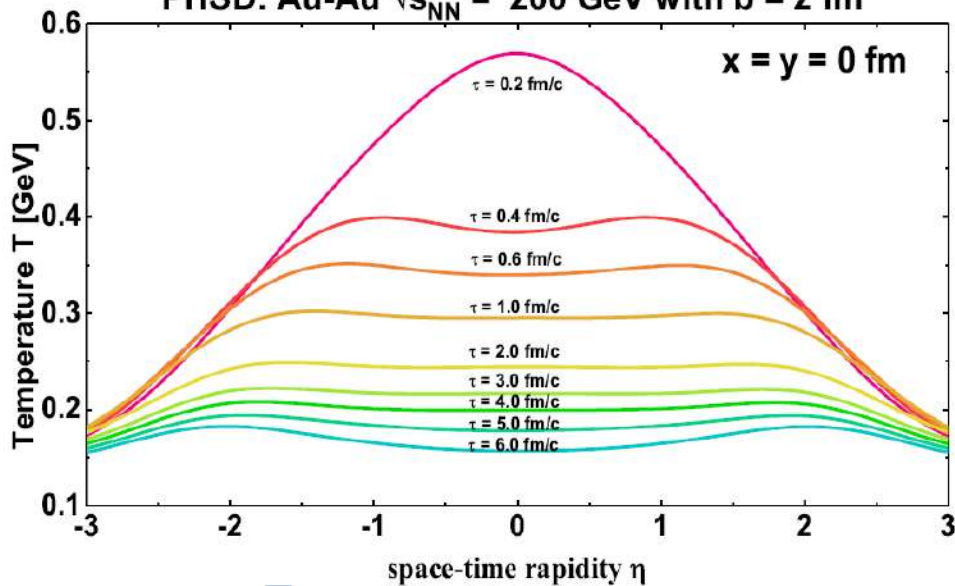
*Cf. talk by Takeshi Kodama*



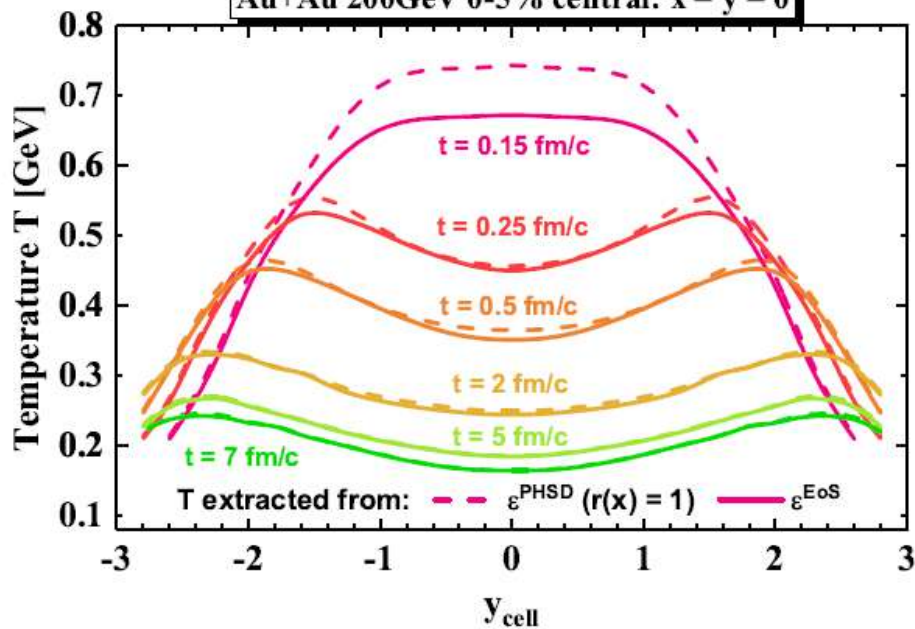
# T, P in HIC ( $\sqrt{s_{NN}} = 200$ GeV)



PHSD: Au-Au  $\sqrt{s_{NN}} = 200$  GeV with  $b = 2$  fm



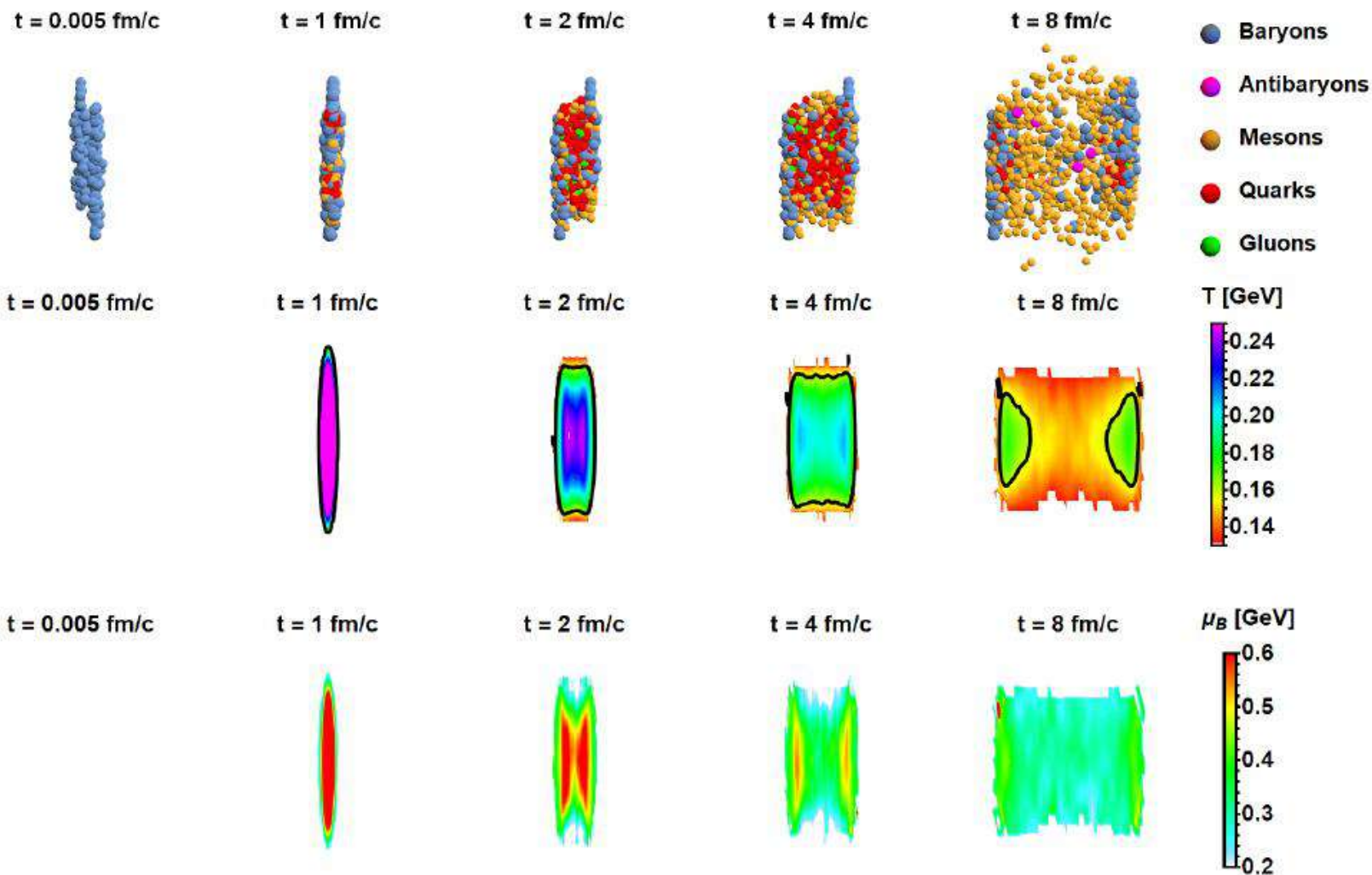
Au+Au 200GeV 0-5% central:  $x = y = 0$



**Milne coordinates ( $\tau, x, y, \eta$ ) : temperature profile - almost boost-invariant**

# Illustration for HIC ( $\sqrt{s_{NN}} = 19.6 \text{ GeV}$ )

Au + Au  $\sqrt{s_{NN}} = 19.6 \text{ GeV}$  –  $b = 2 \text{ fm}$  – Section view





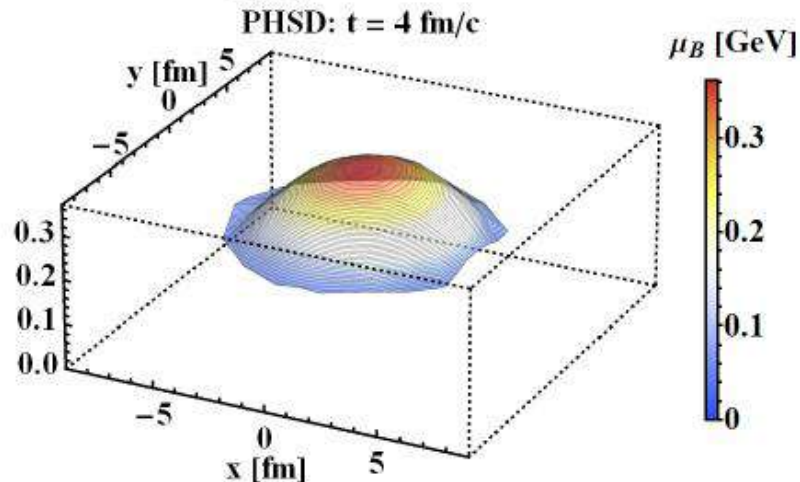
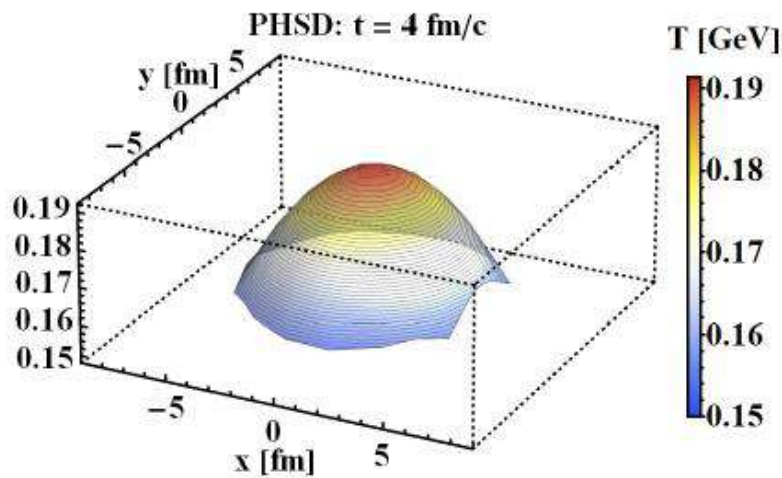
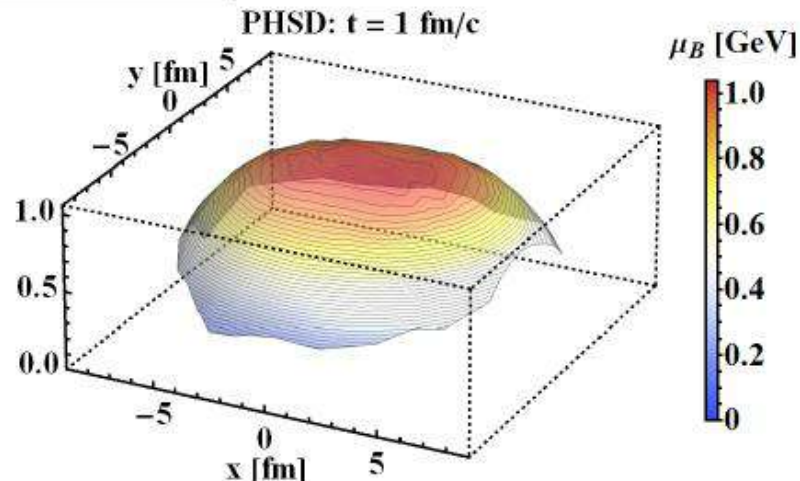
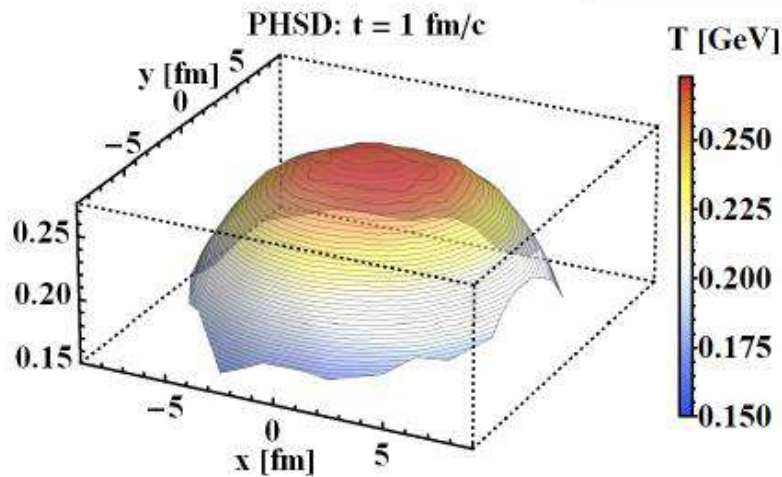
# Illustration for HIC ( $\sqrt{s_{NN}} = 17$ GeV)

The **temperature** profile in (x; y)

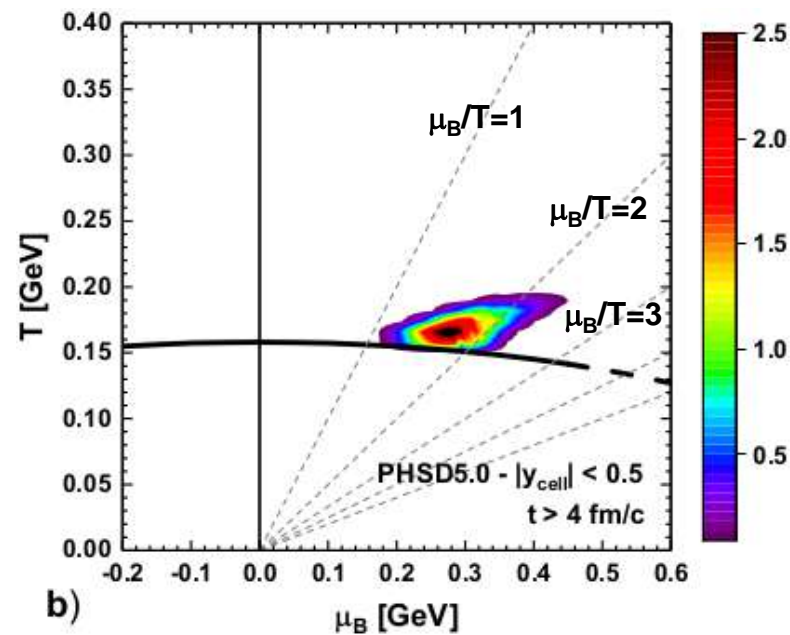
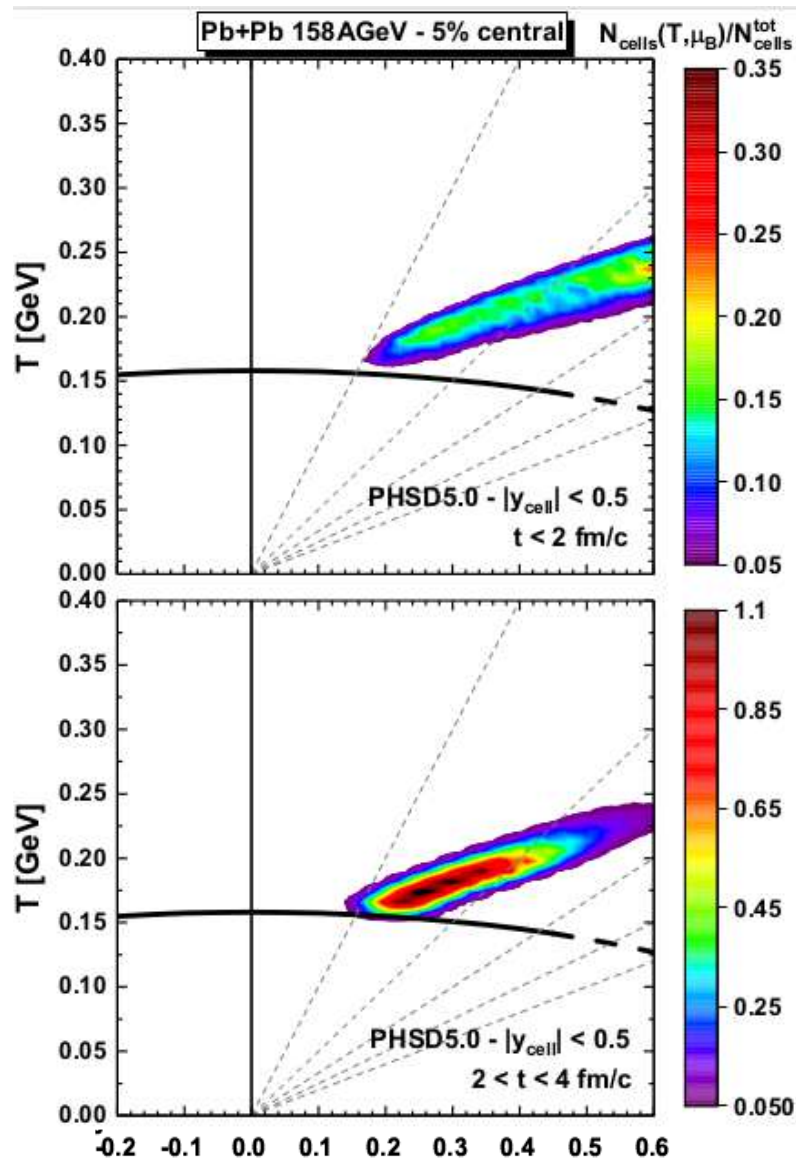
**Baryon chemical potential** profile in (x; y)

at midrapidity ( $|y_{\text{cell}}| < 1$ ) at 1 and 4 fm/c

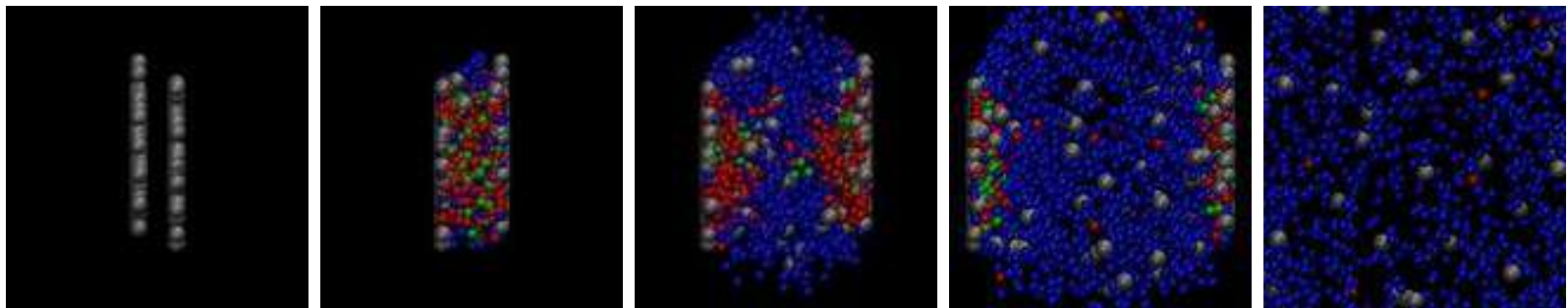
Pb+Pb 158A GeV - 5% central



# Illustration for HIC ( $\sqrt{s_{NN}} = 17$ GeV)



Traces of the QGP at finite  $\mu_q$  in  
observables  
in high energy heavy-ion collisions



# Results for HIC



➤ Comparison between three different results:

1) PHSD 4.0 : only  $\sigma(T)$  and  $\rho(T)$

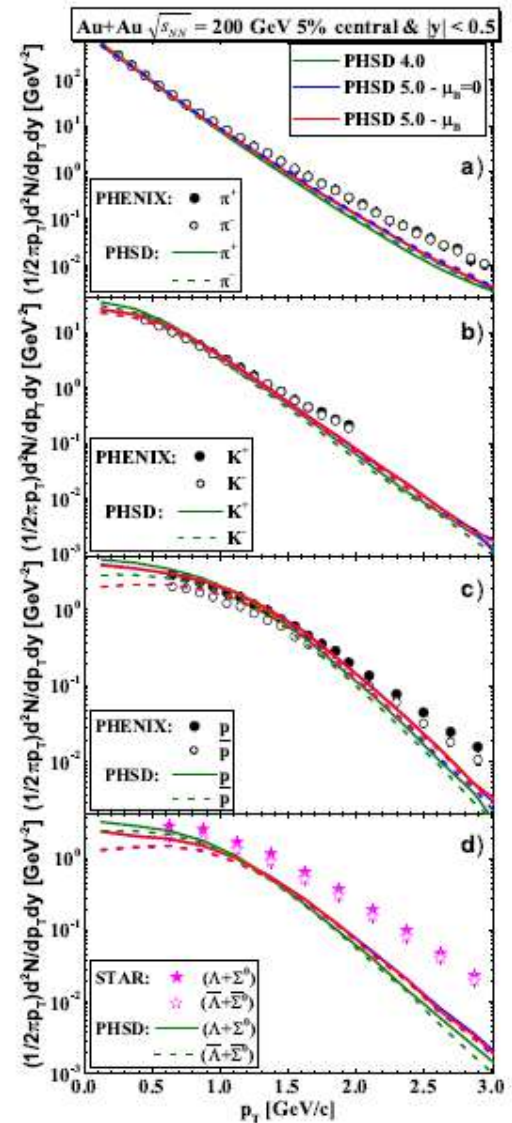
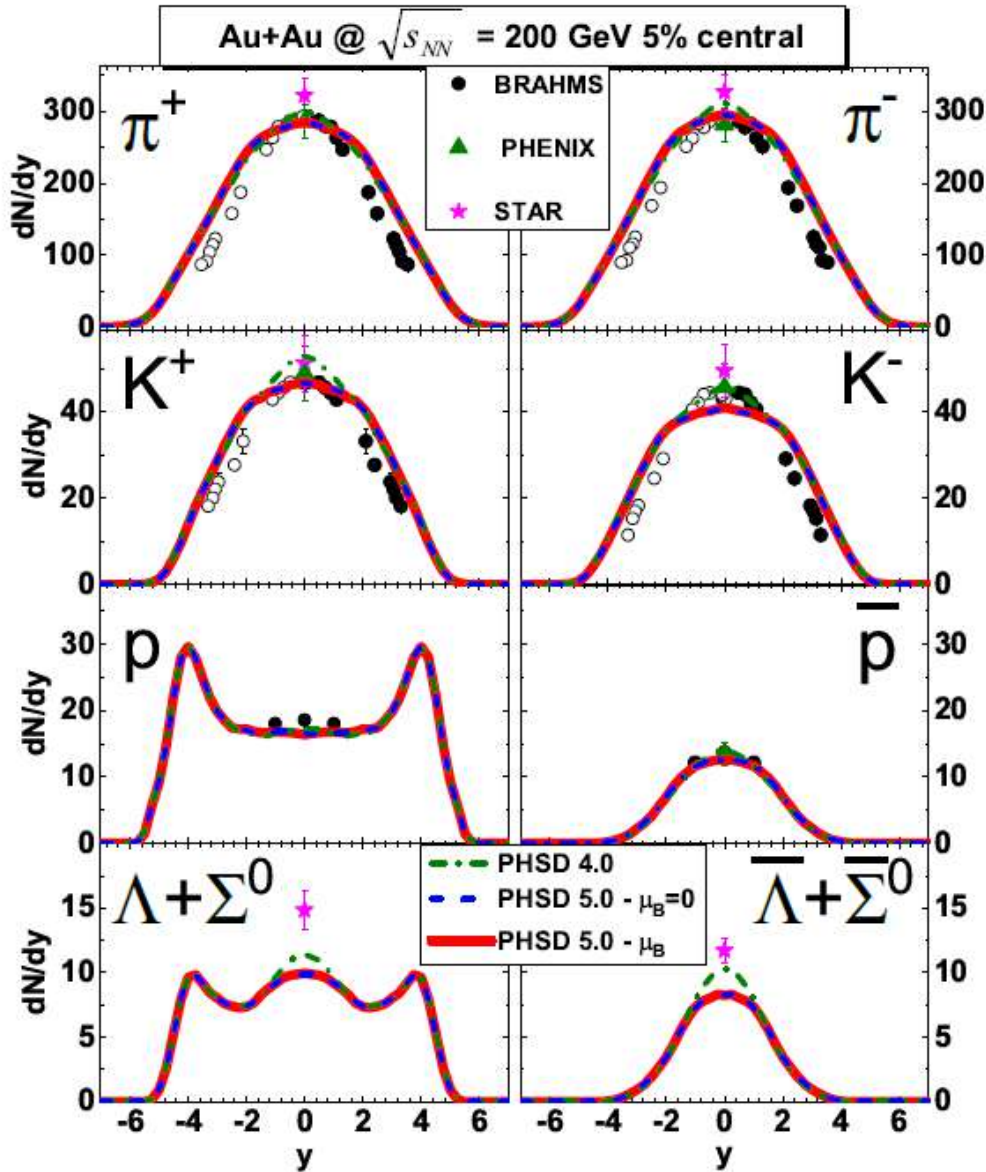
2) PHSD 5.0 : with  $\sigma(\sqrt{s}, T, \mu_B = 0)$  and  $\rho(T, \mu_B = 0)$

3) PHSD 5.0 : with  $\sigma(\sqrt{s}, T, \mu_B)$  and  $\rho(T, \mu_B)$

$\rho$ -spectral function  
→ (mass and width)

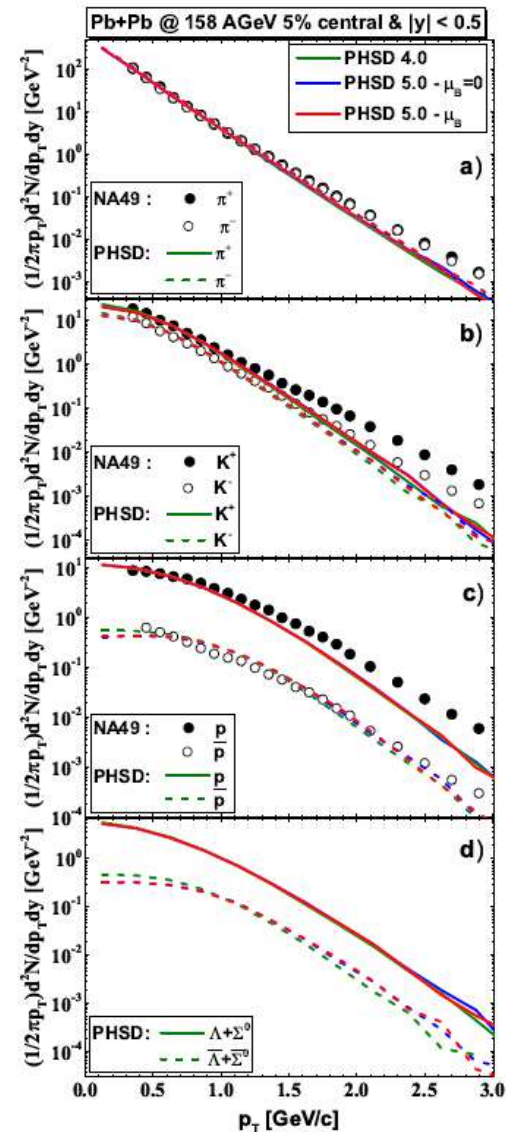
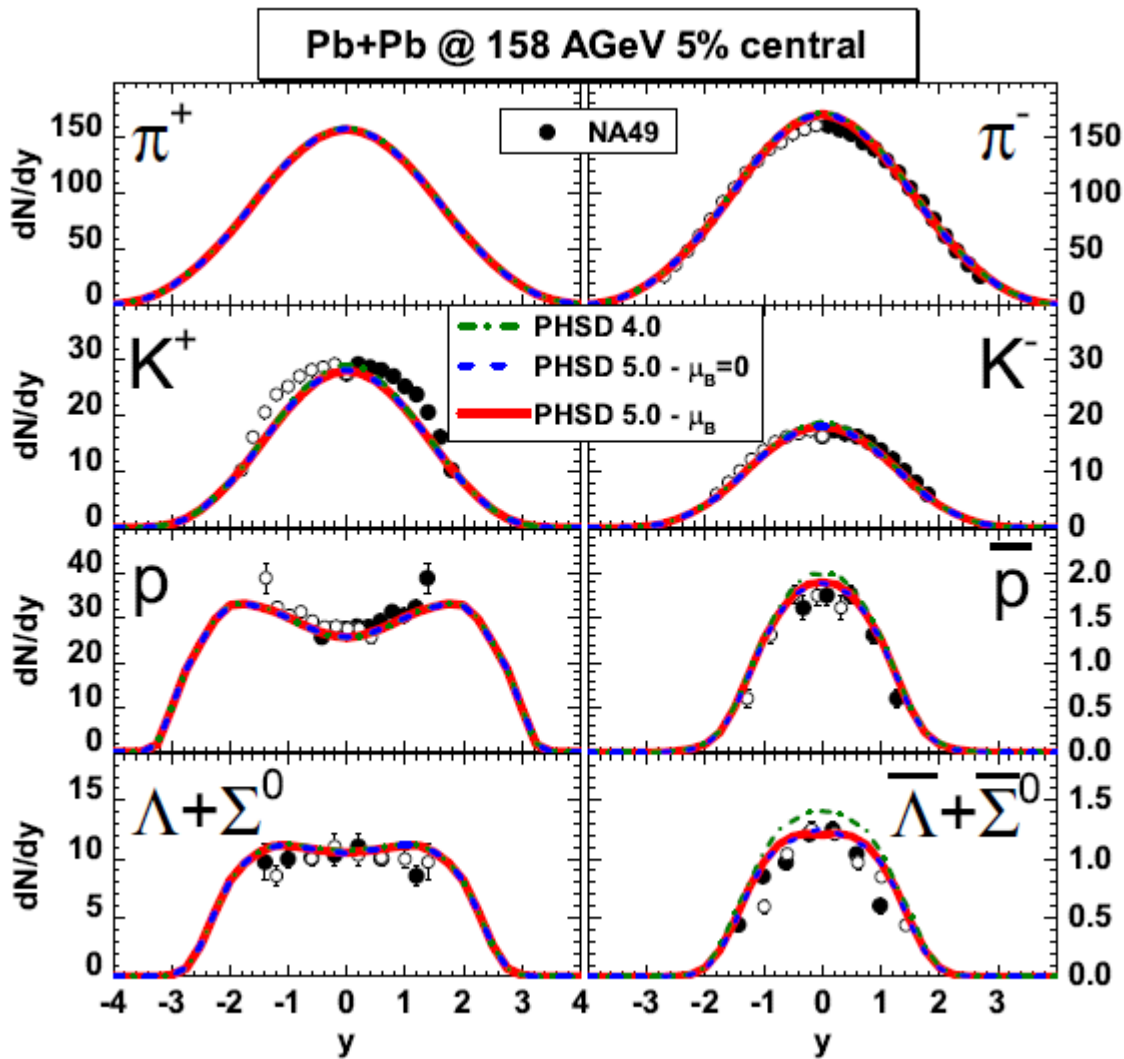


# Results for HIC ( $\sqrt{s_{NN}} = 200$ GeV)



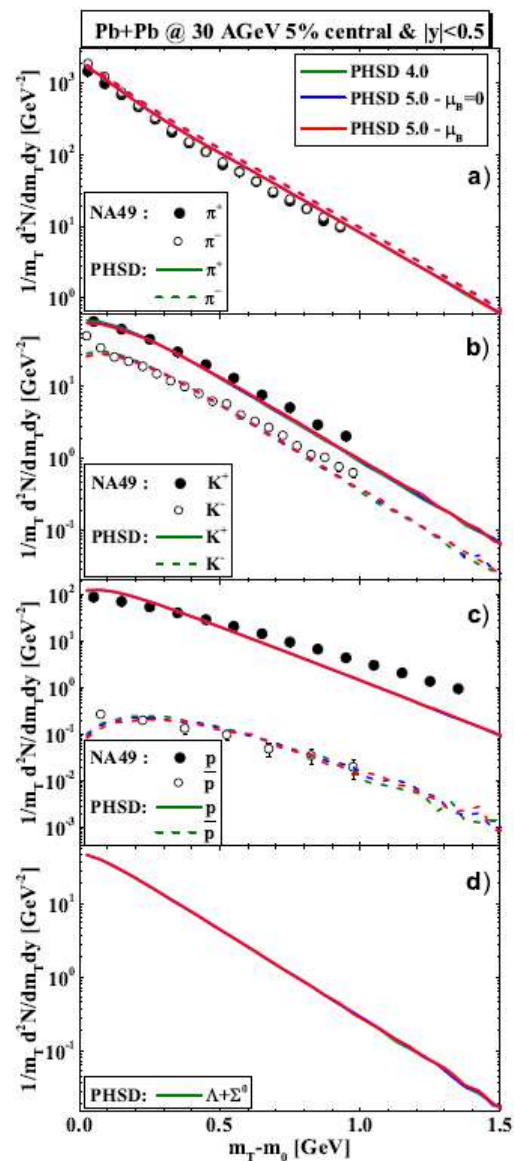
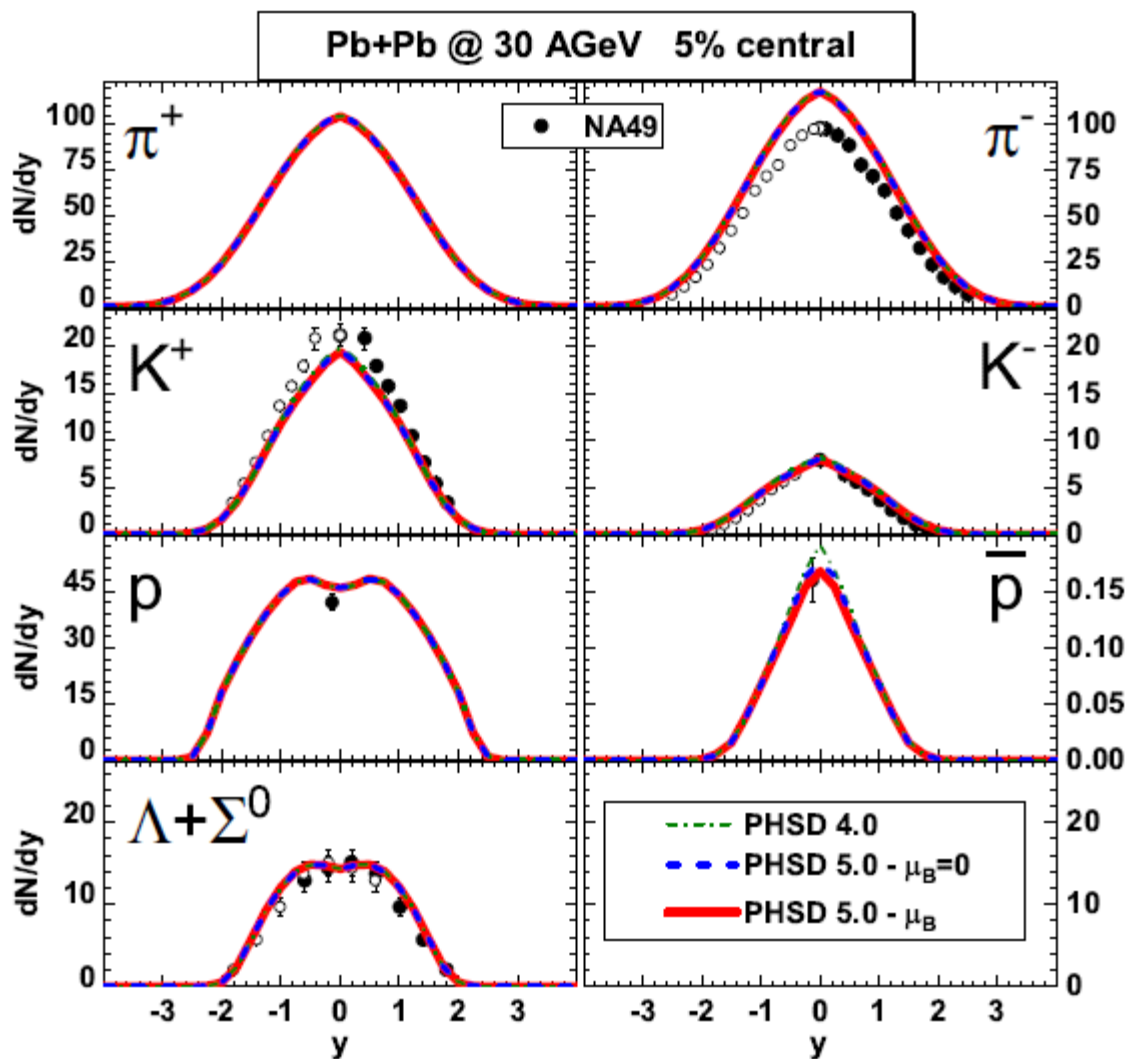


# Results for HIC ( $\sqrt{s_{NN}} = 17$ GeV)



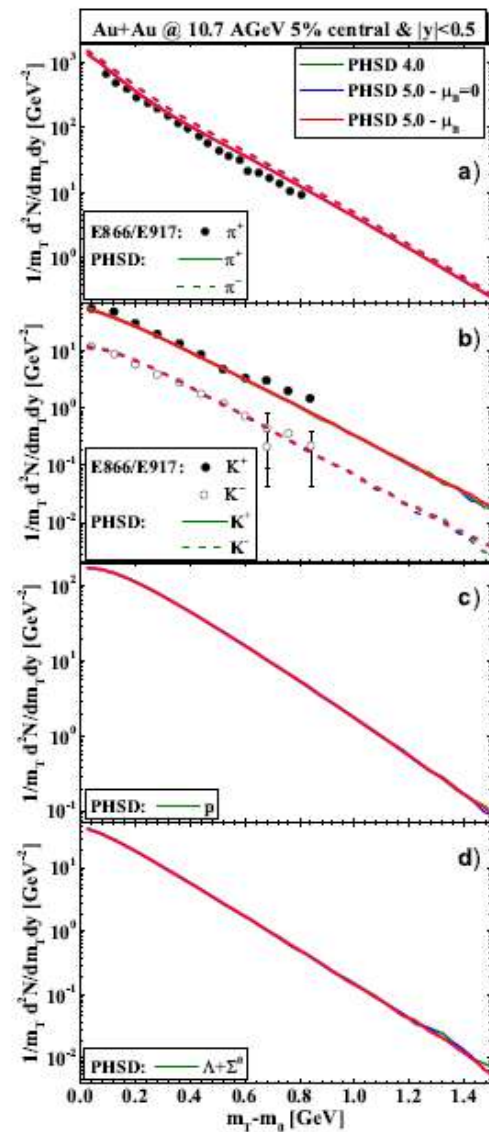
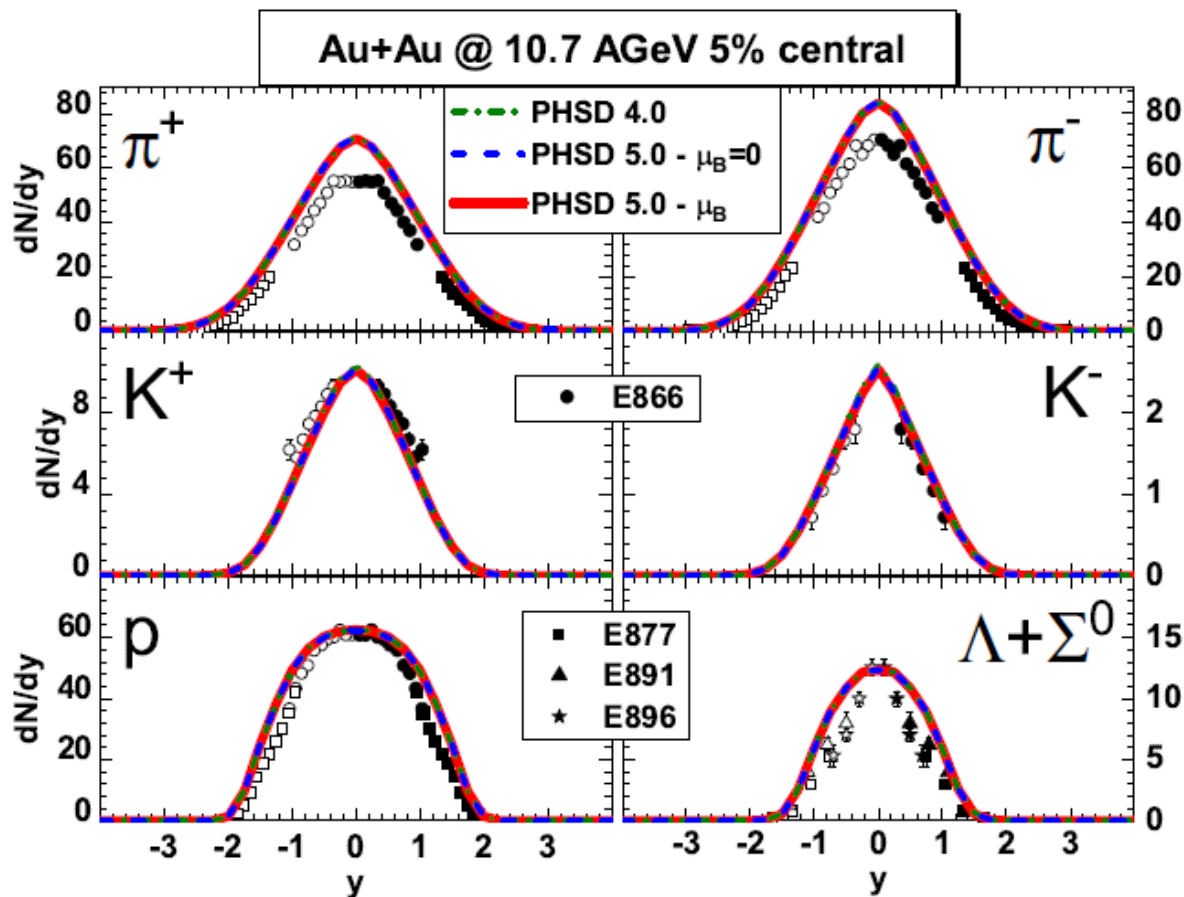


# Results for HIC ( $\sqrt{s_{NN}} = 7.6$ GeV)



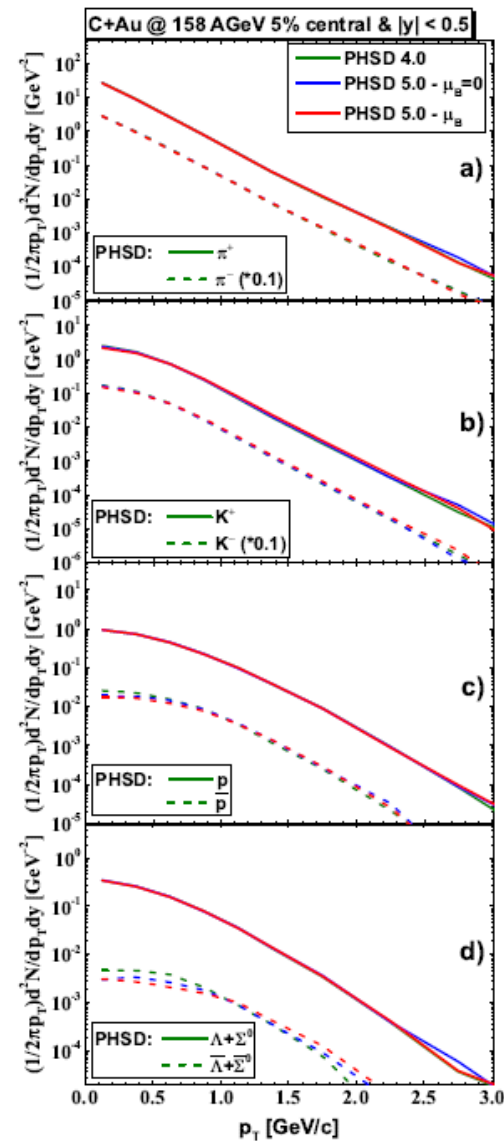
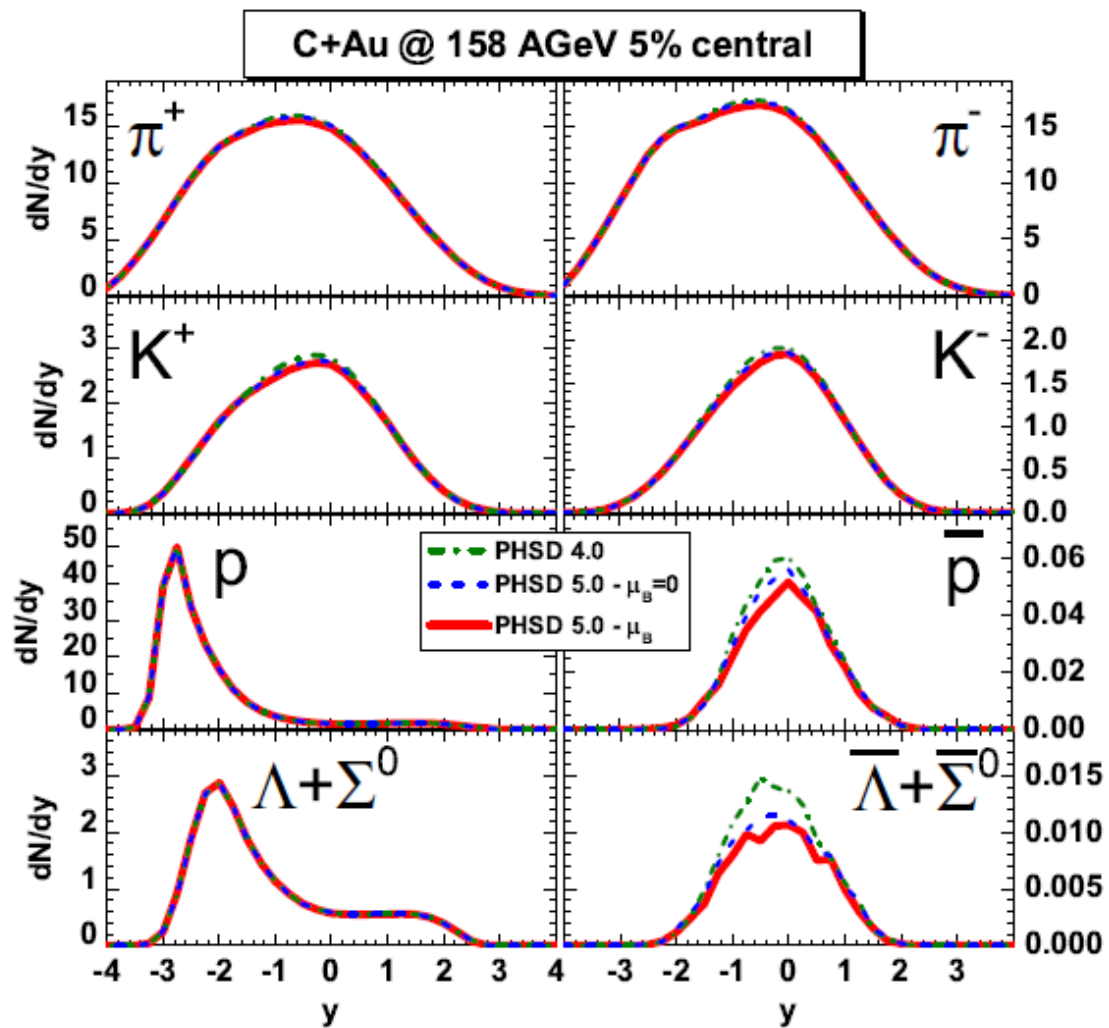


# Results for HIC ( $\sqrt{s_{NN}} = 4.86$ GeV)





# Results for asymmetric systems





# Summary / Outlook

- ❑  **$(T, \mu_B)$ -dependent** cross sections and masses/widths of quarks and gluons have been implemented in PHSD
- ❑ **High- $\mu_B$**  regions are probed at **low  $\sqrt{s_{NN}}$**  or **high rapidity** regions
- ❑ But, QGP fraction is **small** at low  $\sqrt{s_{NN}}$  :
  - ➔ no effects seen in **bulk observables**
  
- ❑ **Outlook:**
  - Study more sensitive probes to finite- $\mu_B$  dynamics
  - More precise EoS finite/large  $\mu_B$
  - Possible 1<sup>st</sup> order phase transition at large  $\mu_B$ ?!